

# Answer Set Programming for Stream Reasoning

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# Outline

- 1 Introduction
- 2 Sliding Windows
- 3 Advanced Modeling
- 4 Conclusion

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# Motivation

While traditional Answer Set Programming (ASP) methods aim at singular problem solving,

*“stream reasoning, instead, restricts processing to a certain **window of concern**, focusing on a subset of recent statements in the stream, while ignoring previous statements” [BBC<sup>+</sup>10].*

Data stream management systems (for high-throughput stream processing) [GÖ10] lack complex reasoning capacities [DCvF09], as required in application areas like

- ambient assisted living,
- dynamic scheduling,
- robotics,
- etc.

**Goal:** Close gap by enriching ASP with means for stream reasoning!

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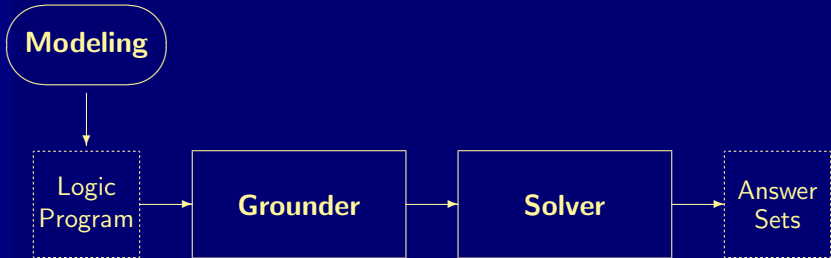
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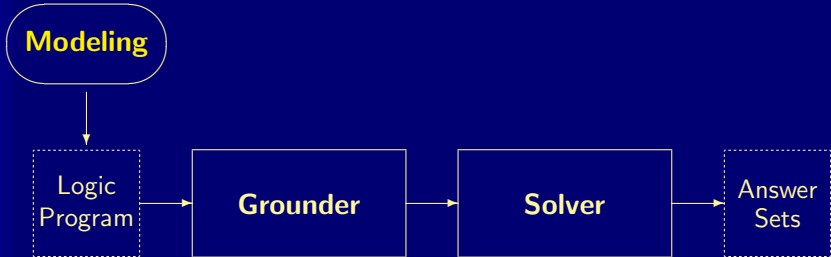
# Setting the stage

## Reactive ASP by oclingo



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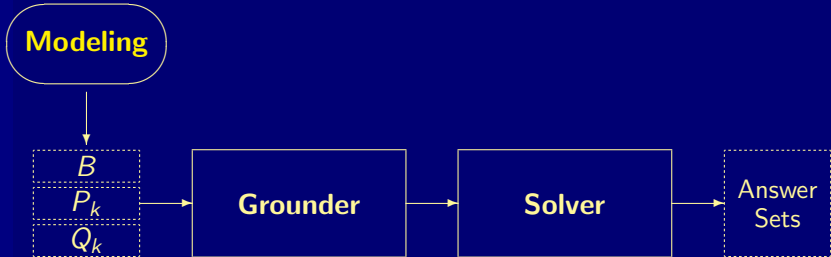
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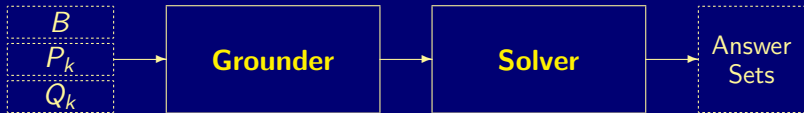
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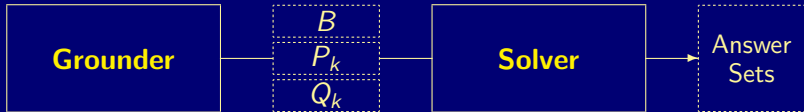
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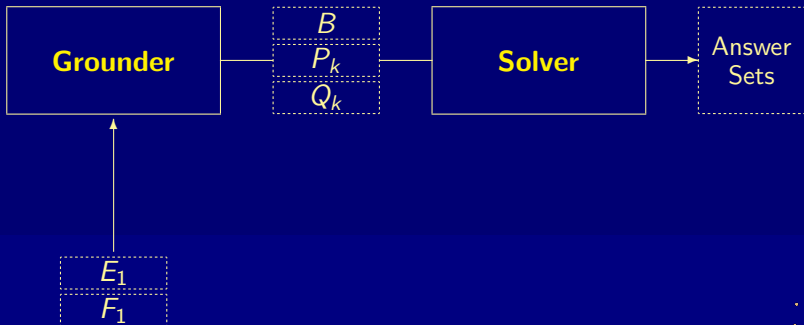
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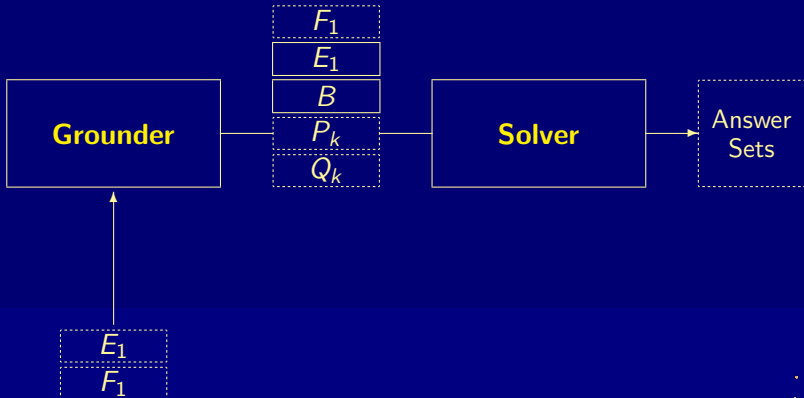
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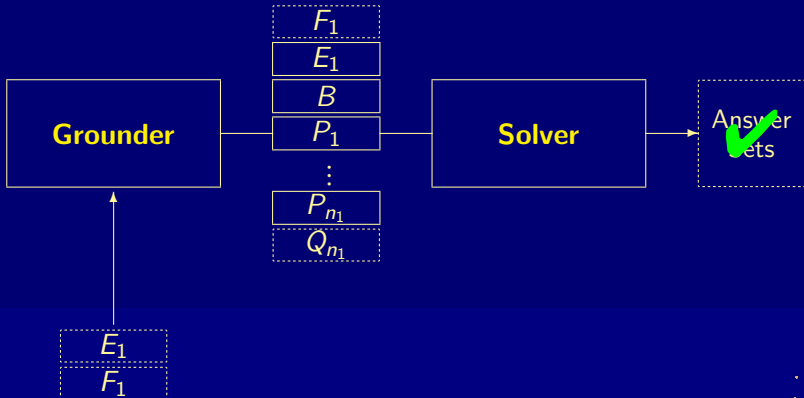
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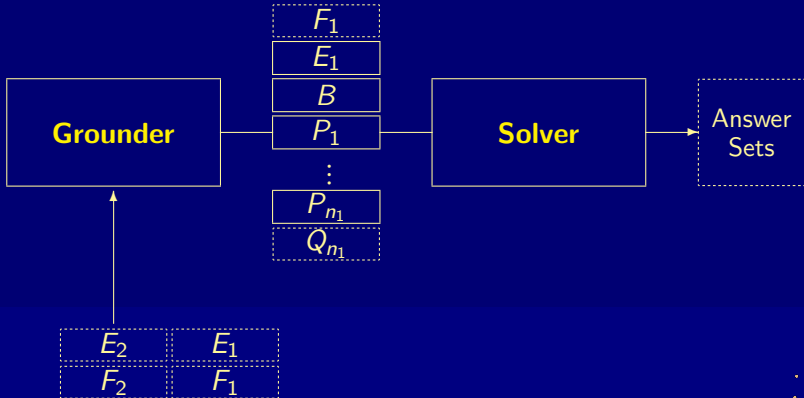
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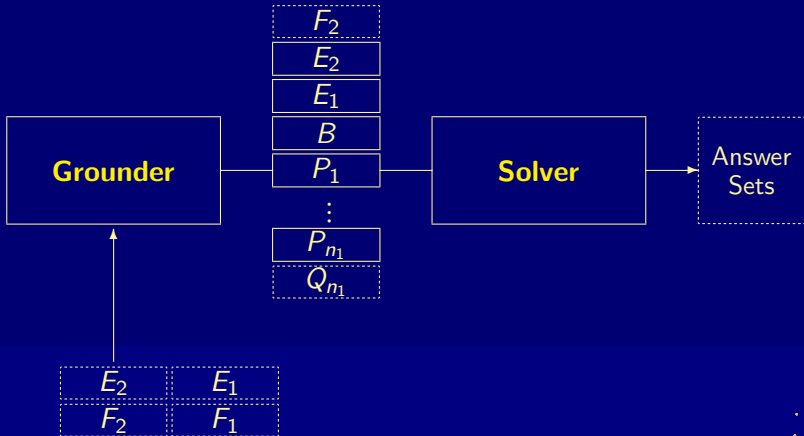
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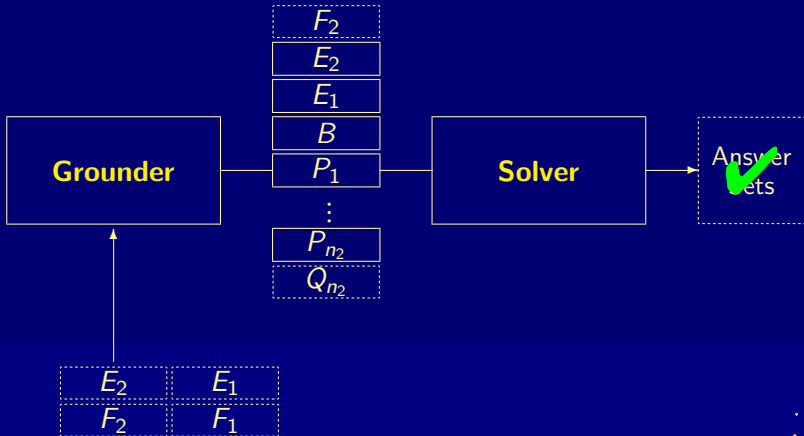
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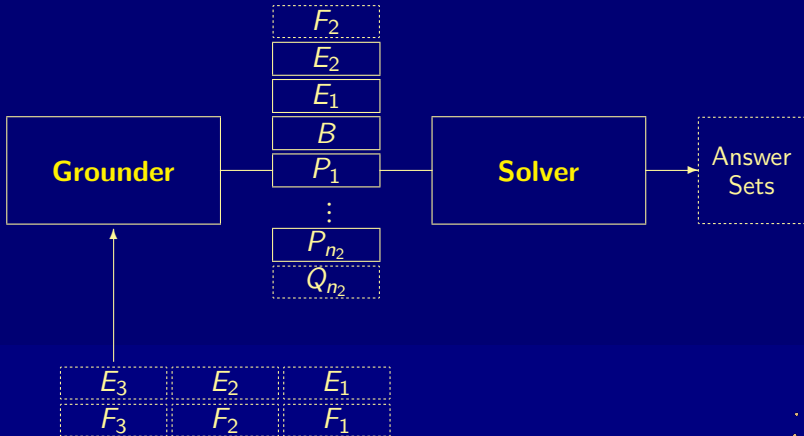
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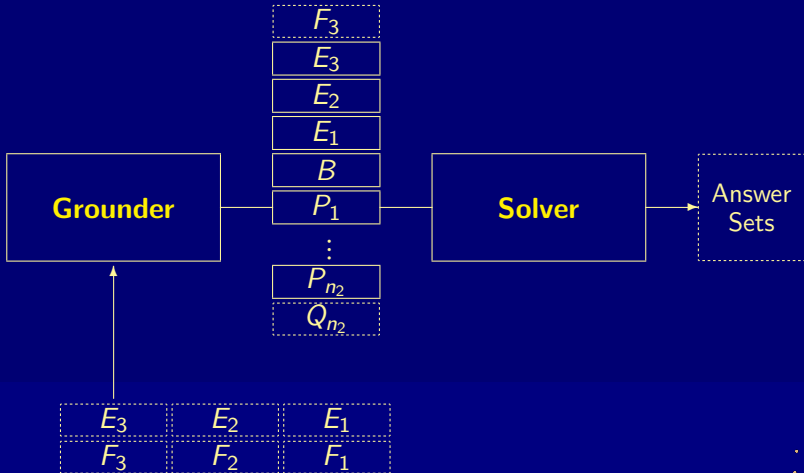
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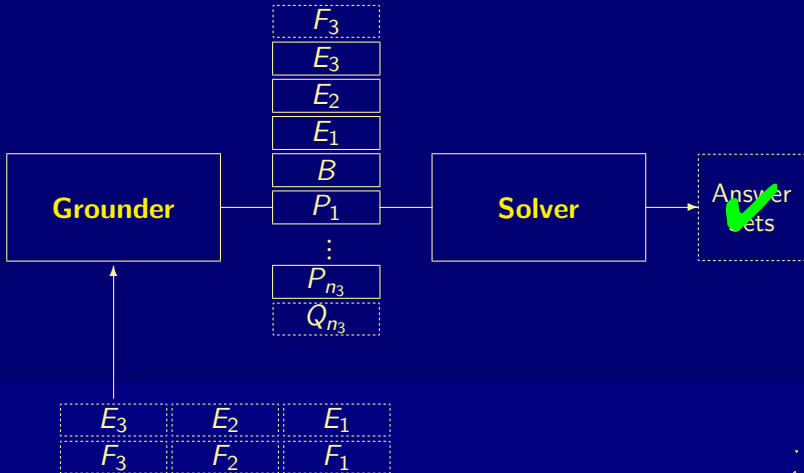
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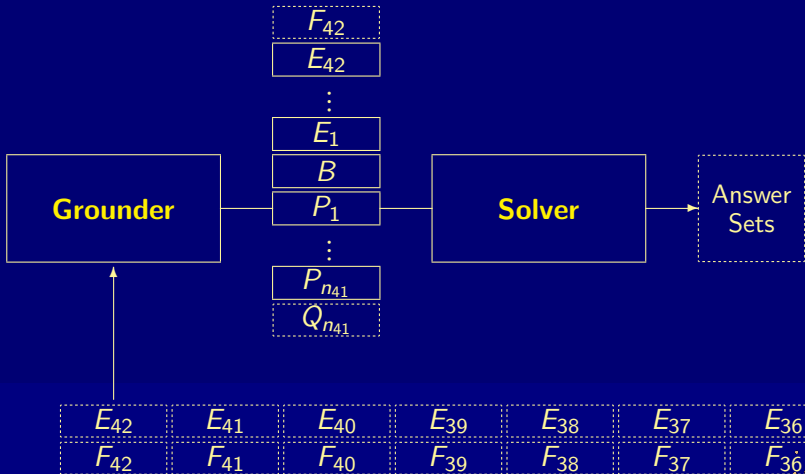
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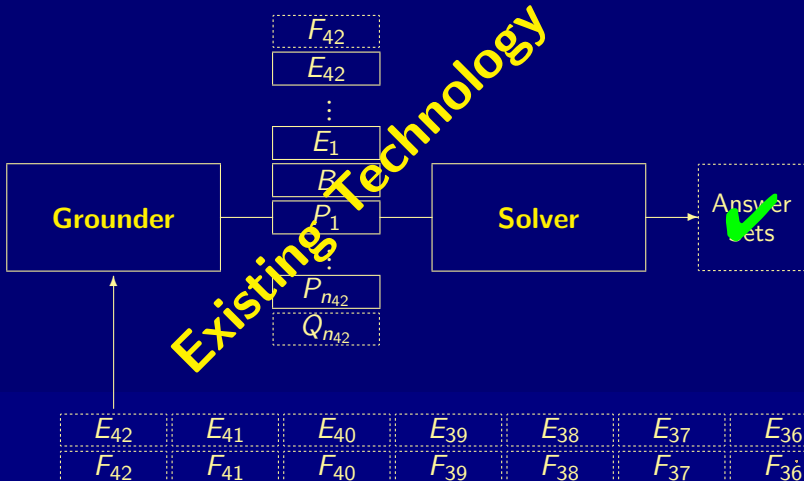
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# Setting the stage

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## Running example

Consider the task of continuously matching stream prefixes against regular expression  $(a|b)^*aa$ .

Example Stream

*aabaaab...* ✗

**Observation:** Only the two last readings are significant.

➡ Restrict attention to sliding window of width 2!



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Consider the task of continuously matching stream prefixes against regular expression  $(a|b)^*aa$ .

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*aa*baaab... ✓

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# Limitations of (foregoing) reactive ASP I

## Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
read(a,1).	read(a,2).	read(b,3).	...
<b>#endstep</b> .	<b>#endstep</b> .	<b>#endstep</b> .	

## Reactive ASP Encoding

```
#iinit 0.  
#cumulative t.          #external read(a;b,t+1).  
accept(t) :- read(a,t;t-1), not read(a;b,t+1).
```

## Incremental Instantiation: $t = 0$

```
accept(0) :- read(a,0), read(a,-1),  
            not read(a,1), not read(b,1).
```

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## Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
read(a,1).	read(a,2).	read(b,3).	...
<b>#endstep</b> .	<b>#endstep</b> .	<b>#endstep</b> .	

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## Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
read(a,1).	read(a,2).	read(b,3).	...
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## Reactive ASP Encoding

```
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<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
read(a,1).	read(a,2).	read(b,3).	...
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#iinit 0.  
#cumulative t.          #external read(a;b,t+1).  
accept(t) :- read(a,t;t-1), not read(a;b,t+1).
```

## Incremental Instantiation: $t = 1$

```
accept(1) :- read(a,1), read(a,0),  
             not read(a,2), not read(b,2).  
read(a,1).
```

# Limitations of (foregoing) reactive ASP I

## Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
read(a,1).	read(a,2).	read(b,3).	...
<b>#endstep</b> .	<b>#endstep</b> .	<b>#endstep</b> .	

## Reactive ASP Encoding

```
#iinit 0.  
#cumulative  $t$ .      #external read(a;b, $t+1$ ).  
accept( $t$ ) :- read(a, $t$ ; $t-1$ ), not read(a;b, $t+1$ ).
```

## Incremental Instantiation: $t = 2$

```
accept(2) :- read(a,2), read(a,1),  
             not read(a,3), not read(b,3).  
read(a,1).  read(a,2).
```

# Limitations of (foregoing) reactive ASP I

## Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
read(a,1).	read(a,2).	read(b,3).	...
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#iinit 0.  
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accept( $t$ ) :- read(a, $t$ ; $t-1$ ), not read(a;b, $t+1$ ).
```

## Incremental Instantiation: $t = 3$

```
accept(3) :- read(a,3), read(a,2),  
             not read(a,4), not read(b,4).  
read(a,1).  read(a,2).  read(b,3).
```

# Limitations of (foregoing) reactive ASP I

## Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
read(a,1).	read(a,2).	read(b,3).	...
<b>#endstep</b> .	<b>#endstep</b> .	<b>#endstep</b> .	

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```
#iinit 0.  
#cumulative t.          #external read(a;b,t+1).  
accept(t) :- read(a,t;t-1), not read(a;b,t+1).
```

## Incremental Instantiation: $t = \dots$

```
...  
read(a,1).   read(a,2).   read(b,3).   ...
```

**✗** Obsolete data is *not* erased!

# Limitations of (foregoing) reactive ASP II

## Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>	
<b>#volatile.</b>	<b>#volatile.</b>	<b>#volatile.</b>	
	read(a,1).	read(a,2).	
read(a,1).	read(a,2).	read(b,3).	...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>	

## Reactive ASP Encoding

```
#iinit 0.  
#cumulative t.           #external read(a;b,t+1).  
accept(t) :- read(a,t;t-1), not read(a;b,t+1).
```

- ✗ Data must be replayed!
- Redefinitions (of head atoms) violate modularity assumption.



# Limitations of (foregoing) reactive ASP II

## Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>	
<b>#volatile.</b>	<b>#volatile.</b>	<b>#volatile.</b>	
read(a,1).	read(a,1).	read(a,2).	
read(a,1).	read(a,2).	read(b,3).	...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>	

## Reactive ASP Encoding

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#cumulative t.          #external read(a;b,t).  
accept(t) :- read(a,t;t-1).
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## Limitations of (foregoing) reactive ASP II

### Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>	
<b>#volatile.</b>	<b>#volatile.</b>	<b>#volatile.</b>	
	<code>read(a,1).</code>	<code>read(a,2).</code>	
<code>read(a,1).</code>	<code>read(a,2).</code>	<code>read(b,3).</code>	<code>...</code>
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>	

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#cumulative t.          #external read(a;b,t).  
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<code>read(a,1).</code>	<code>read(a,2).</code>	<code>read(b,3).</code>	<code>...</code>
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>	

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<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile.</b>	<b>#volatile.</b>	<b>#volatile.</b>
	read(a,1,2).	read(a,2,3).
read(a,1,1).	read(a,2,2).	read(b,3,3). ...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>

### Reactive ASP Encoding

```
#cumulative t.          #external read(a;b,t;t-1,t).  
accept(t) :- read(a,t;t-1,t).
```

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- Redefinitions (of head atoms) violate modularity assumption.

## Limitations of (foregoing) reactive ASP II

### Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile.</b>	<b>#volatile.</b>	<b>#volatile.</b>
	<code>read(a,1,2).</code>	<code>read(a,2,3).</code>
<code>read(a,1,1).</code>	<code>read(a,2,2).</code>	<code>read(b,3,3).</code> ...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>

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```
#cumulative t.          #external read(a;b,t;t-1,t).  
accept(t) :- read(a,t;t-1,t).
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✗ Data must be replayed!

- Redefinitions (of head atoms) violate modularity assumption.

# Closing the gap

## Review

Neither permanent (“**#cumulative.**”) nor singular (“**#volatile.**”) consideration of online data is suitable for stream reasoning.

## Preview

Extend oclingo language by “**#volatile : /.**” directive for built-in support of expiration in *l* steps.

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## Review

Neither permanent (“**#cumulative.**”) nor singular (“**#volatile.**”) consideration of online data is suitable for stream reasoning.

## Preview

Extend oclingo language by “**#volatile : /.**” directive for built-in support of **expiration in / steps.**

## Closing the gap

### Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile : 2.</b>	<b>#volatile : 2.</b>	<b>#volatile : 2.</b>
read(a,1).	read(a,2).	read(b,3). ...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>

### Reactive ASP Encoding

```
#cumulative t.          #external read(a;b,t).  
accept(t) :- read(a,t;t-1).
```

Incremental Instantiation:  $t = 1$

```
accept(1) :- read(a,1), read(a,0).  
             read(a,1).
```

✓ Obsolete data is erased without necessitating replays!



## Closing the gap

### Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.
<b>#volatile</b> : 2.	<b>#volatile</b> : 2.	<b>#volatile</b> : 2.
read(a,1).	read(a,2).	read(b,3). ...
<b>#endstep</b> .	<b>#endstep</b> .	<b>#endstep</b> .

### Reactive ASP Encoding

```
#cumulative t.          #external read(a;b,t).  
accept(t) :- read(a,t;t-1).
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accept(1) :- read(a,1), read(a,0).  
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## Closing the gap

### Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile</b> : 2.	<b>#volatile</b> : 2.	<b>#volatile</b> : 2.
read(a,1).	read(a,2).	read(b,3).     ...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>

### Reactive ASP Encoding

```
#cumulative t.            #external read(a;b,t).  
accept(t) :- read(a,t;t-1).
```

### Incremental Instantiation: $t = 1$

```
accept(1) :- read(a,1), read(a,0).  
          read(a,1).
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## Closing the gap

### Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.
<b>#volatile</b> : 2.	<b>#volatile</b> : 2.	<b>#volatile</b> : 2.
read(a,1).	read(a,2).	read(b,3).     ...
<b>#endstep</b> .	<b>#endstep</b> .	<b>#endstep</b> .

### Reactive ASP Encoding

```
#cumulative t.            #external read(a;b,t).  
accept(t) :- read(a,t;t-1).
```

### Incremental Instantiation: $t = 2$

```
accept(2) :- read(a,2), read(a,1).  
          read(a,2). read(a,1).
```

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## Closing the gap

### Stream Data

<b>#step</b> 1.	<b>#step</b> 2.	<b>#step</b> 3.	
<b>#volatile</b> : 2.	<b>#volatile</b> : 2.	<b>#volatile</b> : 2.	
read(a,1).	read(a,2).	read(b,3).	...
<b>#endstep</b> .	<b>#endstep</b> .	<b>#endstep</b> .	

### Reactive ASP Encoding

```
#cumulative t.           #external read(a;b,t).  
accept(t) :- read(a,t;t-1).
```

### Incremental Instantiation: $t = 3$

```
accept(3) :- read(a,3), read(a,2).  
            read(b,3). read(a,2).
```

✓ Obsolete data is erased without necessitating replays!

## Closing the gap

### Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile</b> : 2.	<b>#volatile</b> : 2.	<b>#volatile</b> : 2.
read(a,1).	read(a,2).	read(b,3). ...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>

### Reactive ASP Encoding

```
#cumulative t.           #external read(a;b,t).  
accept(t) :- read(a,t;t-1).
```

### Incremental Instantiation: $t = \dots$

```
accept(t) :- read(a,t), read(a,t-1).  
            read(_,t). read(_,t-1).
```

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## Recapitulation

We have seen how an reactive ASP encoding can be **expanded** relative to sliding window data by successively

- 1 generating new (ground) rules
- 2 defining new (ground) atoms.

**✗** New propositions handicap the re-use of conflict constraints.

In what follows, we develop modeling approaches to combine online data with a static problem representation.

**Idea:** Encode problem wrt. any window contents and dynamically map stream data (in window) to internal representation!

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We have seen how an reactive ASP encoding can be expanded relative to sliding window data by successively

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**Idea:** Encode problem wrt. any window contents and dynamically map stream data (in window) to internal representation!



## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

Example Stream

*aabaaab...* ✗

↓↓↓↓↓↓↓ ↓

1234567...

**Observation:** Readings remain in window for five steps.

- ➡ Map stream positions to slots represented by remainders of 5?
- ✗ Circular subsequences may lead to false positives.

**Idea:** Introduce a free slot to disconnect present from past data!

Static problem representation captures windows of width 5.

## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aabaaab...* ❌

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

1 2 3 4 5 6 7 ...

**Observation:** Readings remain in window for five steps.

- ➡ Map stream positions to slots represented by remainders of 5?
- ❌ Circular subsequences may lead to false positives.

**Idea:** Introduce a free slot to disconnect present from past data!

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## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aa***baaab...** ✗

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

1 2 3 4 5 6 7 ...

**Observation:** Readings remain in window for five steps.

- ➡ Map stream positions to slots represented by remainders of 5?
- ✗ Circular subsequences may lead to false positives.

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Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aabaaab...* ✗

↓↓↓↓↓↓↓ ↓

1234567...

**Observation:** Readings remain in window for five steps.

- ➡ Map stream positions to slots represented by remainders of 5?
- ✗ Circular subsequences may lead to false positives.

**Idea:** Introduce a free slot to disconnect present from past data!

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Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aaba*aab... ✗

↓↓↓↓↓↓↓ ↓

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### Example Stream

*aabaaab...* ✗

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

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**Observation:** Readings remain in window for five steps.

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## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aabaaa*b... ✓

↓↓↓↓↓↓↓ ↓

1234567...

**Observation:** Readings remain in window for five steps.

- ➡ Map stream positions to slots represented by remainders of 5?
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Static problem representation captures windows of width 5.

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Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aabaaab*... ✓

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

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**Observation:** Readings remain in window for five steps.

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Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aabaaab...* ✗

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

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Static problem representation captures windows of width 5.

## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include `aaa` as a subsequence.

### Example Stream

`aabaaab...` ✗

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

`1234012...`

**Observation:** Readings remain in window for five steps.

➡ Map stream positions to **slots** represented by remainders of 5?

✗ Circular subsequences may lead to false positives.

**Idea:** Introduce a free slot to disconnect present from past data!

Static problem representation captures windows of width 5.

## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include `aaa` as a subsequence.

### Example Stream

`aabaaab...` ✗

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

1 2 3 4 0 1 2 ...

**Observation:** Readings remain in window for five steps.

➡ Map stream positions to **slots** represented by remainders of 5?

✗ Circular subsequences may lead to false positives.

**Idea:** Introduce a free slot to disconnect present from past data!

Static problem representation captures windows of width 5.

## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include  $aaa$  as a subsequence.

### Example Stream

*aabaaab...* ✗

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

1234501...

**Observation:** Readings remain in window for five steps.

➡ Map stream positions to **slots** represented by remainders of 5?

✗ Circular subsequences may lead to false positives.

**Idea:** Introduce a free slot to disconnect present from past data!

✓ Static problem representation captures windows of width 5.

## Modified running example

Consider the task of checking whether the last five readings (over alphabet  $\{a, b\}$ ) from a stream include *aaa* as a subsequence.

### Example Stream

*aabaaab...* ✗

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1 2 3 4 5 0 1 ...

**Observation:** Readings remain in window for five steps.

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# Static “free slot” approach

## Reactive ASP Encoding

**#base.**

```
next(T,(T+1) #mod 6) :- T := 0..5.  
{ b_read(a,T) } :- next(T,_).  
single(T) :- b_read(a,T).  
double(T) :- b_read(a,T), single(S), next(S,T).  
accept      :- b_read(a,T), double(S), next(S,T).
```

- Static program part is **instantiated once** (initially).
- Successive slots are determined via modulo-6 arithmetic.
- Internal representation of readings is generated by choice rules.
- Subsequences *aaa* are traced wrt. internal representation.
- ➡ Dynamic parts must map readings to internal representation!

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**#base.**

**next**(T,(T+1) **#mod** 6) :- T := 0..5.

{ **b\_read**(a,T) } :- **next**(T,\_).

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**double**(T) :- **b\_read**(a,T), **single**(S), **next**(S,T).

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`accept :- b_read(a,T), double(S), next(S,T).`

## Ground Instantiation

`next(0,1). next(3,4).`

`next(1,2). next(4,5).`

`next(2,3). next(5,0).`



# Static “free slot” approach

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`next(T,(T+1) #mod 6) :- T := 0..5.`

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# Online data vs. internal representation

## Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile</b> : 5.	<b>#volatile</b> : 5.	<b>#volatile</b> : 5.
read(a,1).	read(a,2).	read(b,3). ...
<b>#endstep.</b>	<b>#endstep.</b>	<b>#endstep.</b>

`read  $\Rightarrow$  b_read`

**#cumulative** *t*.            **#external** read(a;b,t).  
:- read(a,t), **not** b\_read(a,t **#mod** 6).

`b_read  $\Rightarrow$  read`

**#volatile** *t* : 6.  
:- b\_read(a,t **#mod** 6), **not** read(a,t).

➡ Constraints expire when window progresses (by six steps).

# Online data vs. internal representation

## Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile</b> : 5.	<b>#volatile</b> : 5.	<b>#volatile</b> : 5.
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read  $\Rightarrow$  b\_read

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#cumulative t.           #external read(a;b,t).  
:- read(a,t), not b_read(a,t #mod 6).
```

b\_read  $\Rightarrow$  read

```
#volatile t : 6.           #iinit -4.  
:- b_read(a,(t+6) #mod 6), not read(a,t).
```

➡ Window is filled at step 1 to avoid guesses (over b\_read).

# Online data vs. internal representation

## Stream Data

<b>#step 1.</b>	<b>#step 2.</b>	<b>#step 3.</b>
<b>#volatile</b> : 5.	<b>#volatile</b> : 5.	<b>#volatile</b> : 5.
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```

**Observation:** Dynamic parts confined to data and its mapping.



## Remodified running example

Consider the task of checking whether the last five readings (over an arbitrary alphabet) include at least three occurrences of letter *a*.

➡ We may use **frame axioms** [Lif02] in the static program part.

### Reactive ASP Encoding

```
#base.  
next(T,(T+1) #mod 5) :- T := 0..4.  
{ b_read(a,T) } :- next(T,_).  
single(T) :- b_read(a,T).  
double(T) :- b_read(a,T), single(S), next(S,T).  
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single(T) :- single(S), next(S,T).  
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**Observation:** Frame axioms propagate into the past (via *next*).

**Idea:** Introduce a predicate to disconnect present from the past!



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### Reactive ASP Encoding *with Frame Axioms*

```
#base.  
next(T,(T+1) #mod 5) :- T := 0..4.  
{ b_read(a,T) } :- next(T,_).  
single(T) :- b_read(a,T).  
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# Static “last slot” approach

## Reactive ASP Encoding with Frame Axioms

```
#base.                                slot(0..4).
next(T,(T+1) #mod 5) :- T := 0..4.
{ b_read(a,T) } :- next(T,_).
single(T) :- b_read(a,T).
double(T) :- b_read(a,T), single(S), next(S,T).
accept    :- b_read(a,T), double(S), next(S,T).
single(T) :- single(S), next(S,T).
double(T) :- double(S), next(S,T).
{ now(T) : slot(T) } 1.
#volatile t.
:- not now(t #mod 5).
```

➡ Propagation beyond the current slot is suppressed (via now).

# Static “last slot” approach

## Reactive ASP Encoding with Frame Axioms

```
#base.                slot(0..4).
next(T,(T+1) #mod 5) :- slot(T), not now(T).
{ b_read(a,T) } :- slot(T).
single(T) :- b_read(a,T).
double(T) :- b_read(a,T), single(S), next(S,T).
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# Outline

- 1 Introduction
- 2 Sliding Windows
- 3 Advanced Modeling
- 4 Conclusion

# Summary

We have

- 1 extended `oclingo` by built-in support of sliding windows and
- 2 developed modeling approaches to reason over transient data.

To promote the re-use of conflict constraints, we proposed to

- 1 statically encode a task wrt. any window contents and
- 2 dynamically map stream data to its designated representation.

We demonstrated how to preserve the chronology of data via

- 1 a free slot in the static program part or
- 2 a predicate qualifying the current slot.

➡ Beyond simple illustration domains [GGK<sup>+</sup>12a, GGK<sup>+</sup>12b], the presented modeling approaches are of general applicability, especially to solve combinatorial problems wrt. stream data.

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# Outlook

While ASP offers interesting prospects for knowledge-intense stream reasoning, continuous settings impose particular challenges.

- Improved low-level support of data expiration is needed to avoid memory pollution.
- Yet missing sequential functionalities, such as optimization, must be supplied to incremental and reactive operation modes.
- Provision of handy high-level language constructs is desirable to facilitate the modeling of sliding window scenarios by users.
- Additional control directives, such as `#assert` and `#retract`, may be useful to flexibly (de)activate logic program parts.

This work is only a first step towards ASP-based stream reasoning.

- ➡ Realistic applications must be pioneered to furnish a deeper understanding and advanced system support of use cases.

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