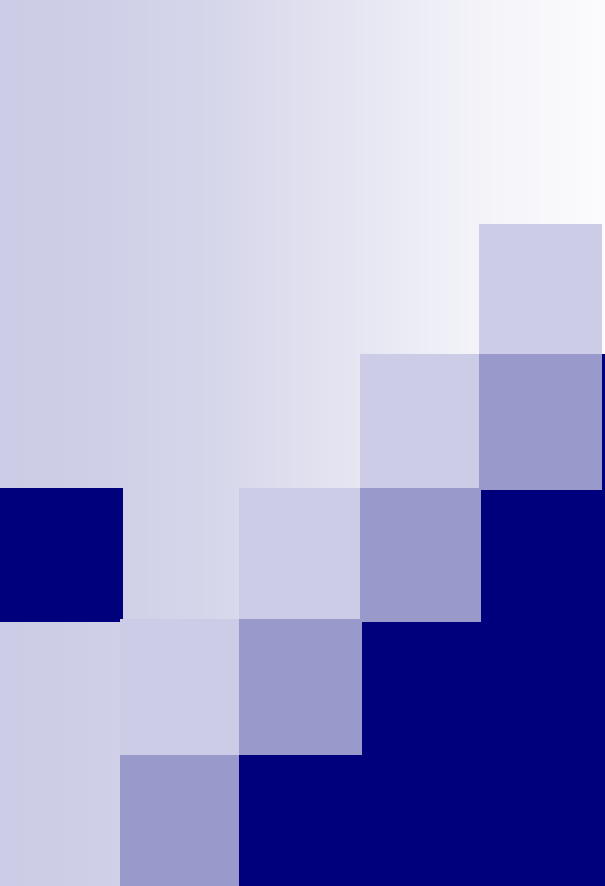


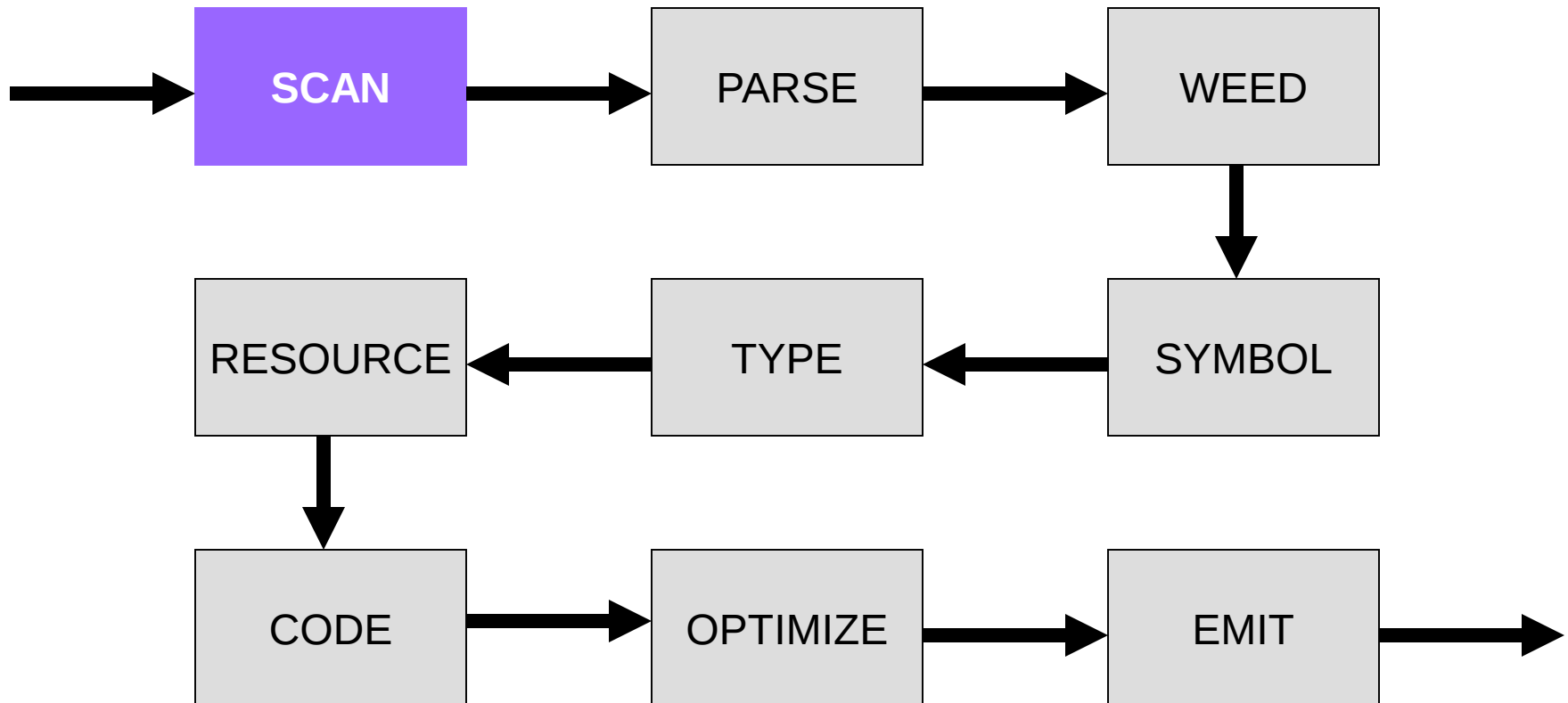


# Compiler

## Scanning

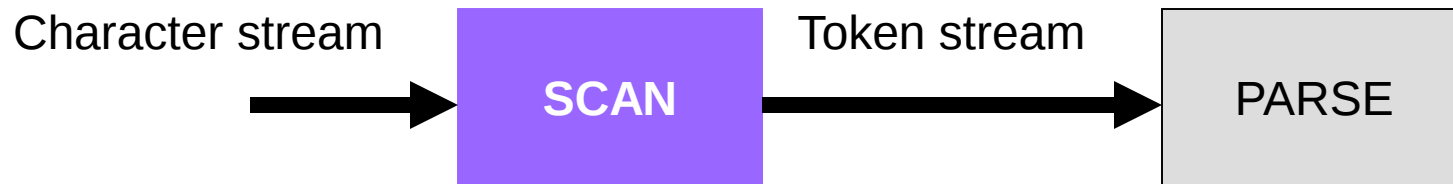
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# Compiler Architecture



# Compiler Architecture

## Source Code



# Scanner: Overview

- A **scanner** transforms a string of characters into a string of *symbols/tokens*:
  - it corresponds to a *finite-state machine* (FSM);
  - plus some code to make it work;
  - FSM can be generated from specification.
- **Symbols** (*a.k.a.* **tokens**, **lexemes**) are the **indivisible units** of a languages syntax
  - key words, punctuation symbols, identifiers ...
- A FSM recognizes the structure of a symbol
  - that structure is specified as a regular expression

# Token Definitions

Described in language specification, e.g.:

“An *identifier* is an unlimited-length sequence of *Java letters* and *Java digits*, the first of which must be a Java letter.

An identifier cannot have the same spelling (Unicode character sequence) as a keyword (§3.9), Boolean literal (§3.10.3), or the null literal (§3.10.7).”

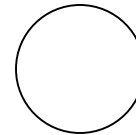
<http://docs.oracle.com/javase/specs/>

# Finite State Machine (FSM) or Finite State Automaton (FSA)

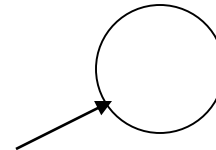
- a quintuple  $(\Sigma, S, s_0, \delta, F)$ , where
  - $\Sigma$ , is a finite non-empty set of symbols (input alphabets)
  - $S$ , is a finite non-empty set of states
  - $s_0 \in S$ , is the initial state
  - $\delta: S \times \Sigma \rightarrow S$ , is the state transition function
  - $F \subseteq S$ , is the (possibly empty) set of accepting (final) states

# FSM Graphs

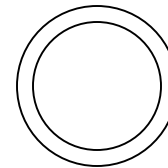
- A state



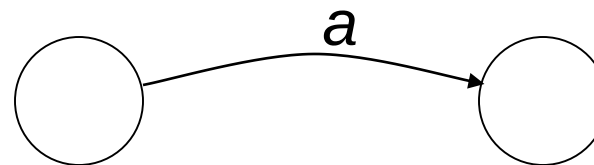
- The start state



- An accepting state



- A transition *a*

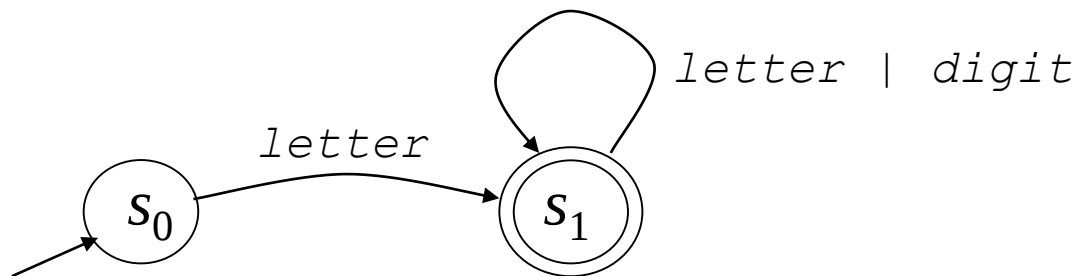


# FSM Interpretation

- Transition:  $s_1 \xrightarrow{a} s_2$
- Is read: in state  $s_1$  on input  $a$  go to state  $s_2$
- At end of input
  - if in accepting state  $\Rightarrow$  *accept*
  - otherwise  $\Rightarrow$  *reject*
- If no transition possible  $\Rightarrow$  *reject*

# Language defined by FSM

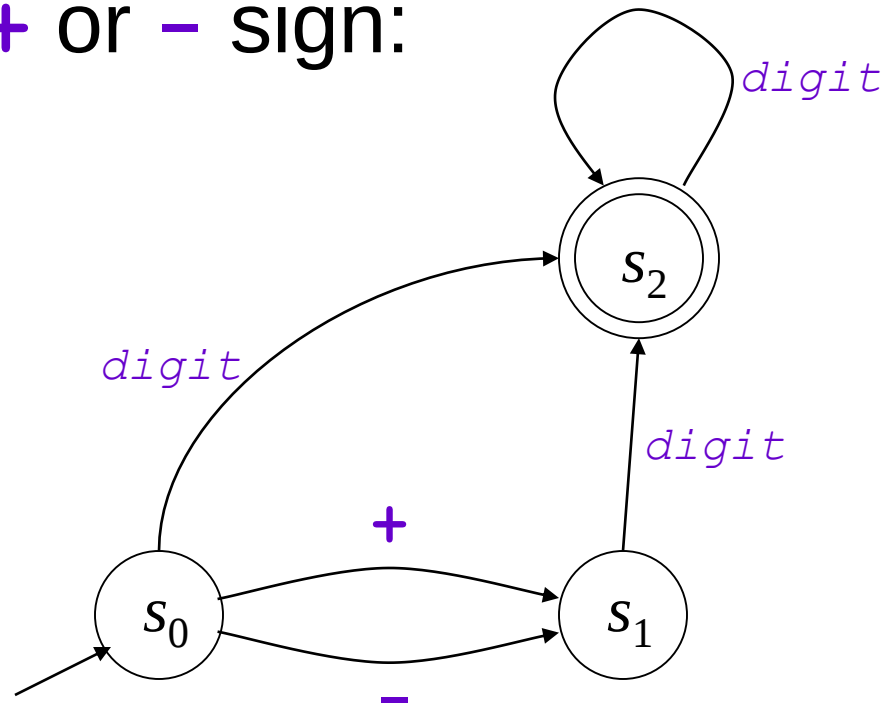
- The *language defined by an FSM* is the set of strings accepted by the FSM.



- in the language of the FSM shown above:
  - `x`, `tmp2`, `XyZzy`, `position27`.
- *not* in the language of the FSM shown above:
  - `123`, `a?`, `13apples`.

# Example: Integer Literals

- FSM that accepts integer literals with an optional **+** or **-** sign:



# Two kinds of FSM

## Deterministic (DFA):

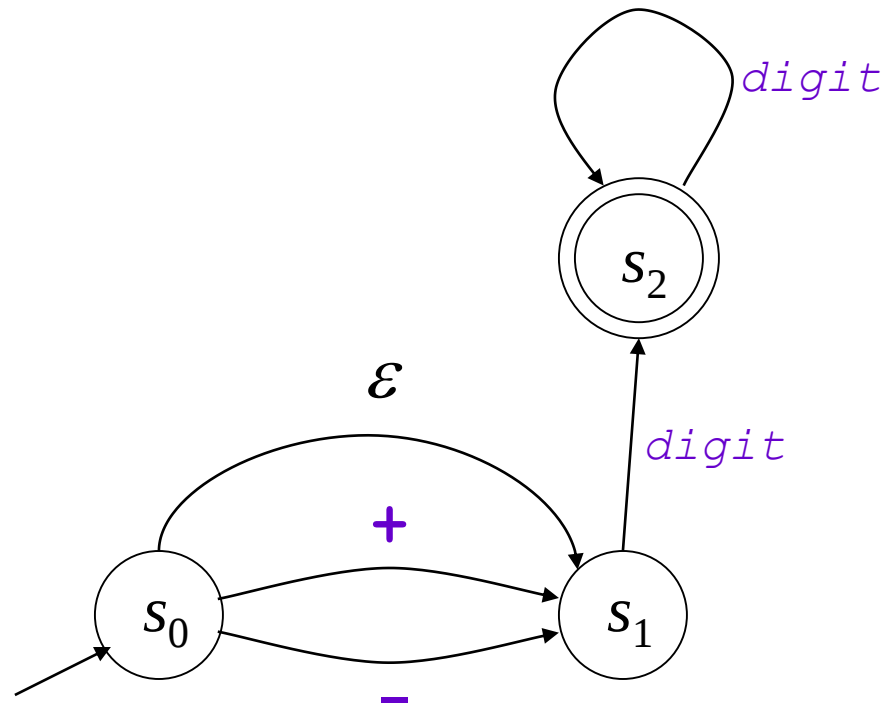
- No state has more than one outgoing edge with the same label.

## Non-Deterministic (NFA):

- States *may have* more than one outgoing edge with the same label.
- Edges may be labeled with  $\varepsilon$  (epsilon), the empty string.
- The automaton can take an  $\varepsilon$  transition *without looking* at the current input character.

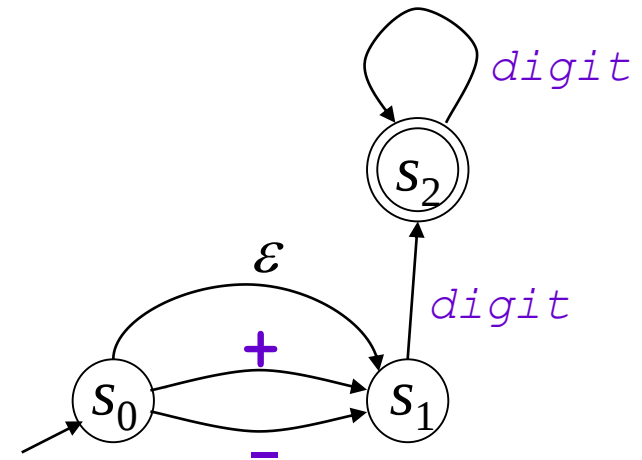
# Example of NFA

## ■ integer-literal example:



# NFA

- sometimes simpler than DFA
- can be in **multiple states** at the **same time**
- NFA **accepts** a string if
  - there **exists** a sequence of **moves**
  - **starting** in the **start state**,
  - **ending** in an **accepting state**,
  - that **consumes** the **entire** string.



- Example:
  - the integer-literal NFA on input "+75"

# Equivalence of DFA and NFA

- Theorem:

- For **every non-deterministic** finite-state machine  $M$ , there **exists a *deterministic*** machine  $M'$  such that  $M$  and  $M'$  **accept the *same language***.

- DFA are easy to implement
- NFA are easy to generate from specifications
- Algorithms exist to convert NFA to DFA  
(*see assignments*)

# Regular Expressions (RE)

- Automaton is a good “visual” aid
  - but is not suitable as a specification
- Regular expressions are a suitable *specification*
  - a compact way to define a language that can be accepted by an automaton.
- used as the input to a scanner generator
  - define each token, and also
  - define white-space, comments, etc.
    - these do not correspond to tokens, but must be recognized and ignored.

# Example: Pascal Identifier

- Lexical specification (in English):
  - a letter, followed by zero or more letters or digits.
- Lexical specification (as a regular expression):
  - *letter (letter | digit)\**

|     |                                 |
|-----|---------------------------------|
|     | means "or"                      |
|     | means "followed by"             |
| *   | means zero or more instances of |
| ( ) | are used for grouping           |

# Operands of RE Operators

- Operands are same as labels on the edges of an FSM
  - single characters or  $\varepsilon$
- *letter* is a shorthand for
  - **a** | **b** | **c** | ... | **z** | **A** | ... | **Z**
- *digit* is a shorthand for
  - **0** | **1** | ... | **9**
- sometimes we put the characters in quotes
  - necessary when denoting | \*

# Operator Precedence

| Regular Expression Operator | Analogous Arithmetic Operator | Precedence |
|-----------------------------|-------------------------------|------------|
|                             | plus                          | lowest     |
|                             | times                         | middle     |
| *                           | exponentiation                | highest    |

Consider regular expressions:

*letter letter | digit\**

*letter (letter | digit)\**

# For You To Do

- Describe (in English) the language defined by each of the following regular expressions:

*letter (letter | digit\*)*

*digit digit\* "." digit digit\**

# Example: Integer Literals

- An integer literal with an optional sign can be defined in English as:

“(nothing or + or -) followed by one or more digits”

- The corresponding regular expression is:

$(+|-|\varepsilon) (\textit{digit digit}^*)$

- Convenience operators

$a^+$  is the same as  $a (a)^*$

$a^?$  is the same as  $(a | \varepsilon)$

$( "+" | "-" )^? \textit{digit}^+$

# Language Defined by RE

- Recall: language = set of strings
- Language defined by an automaton
  - the set of strings accepted by the automaton
- Language defined by a regular expression
  - the set of strings that match the expression.

| Regular Exp. $r$ |                     | Corresponding Set of Strings $L(r)$                                                                           |
|------------------|---------------------|---------------------------------------------------------------------------------------------------------------|
| $\epsilon$       |                     | $\{""\}$                                                                                                      |
| $a$              |                     | $\{"a"\}$                                                                                                     |
| $r \ s$          | $a \ b \ c$         | $L(r) \ L(s)$ <span style="float: right;"><math>\{"abc"\}</math></span>                                       |
| $r \   \ s$      | $a \   \ b \   \ c$ | $L(r) \cup L(s)$ <span style="float: right;"><math>\{"a", "b", "c"\}</math></span>                            |
| $r^*$            | $(a \   \ b)^*$     | $L(r)^*$ <span style="float: right;"><math>\{ "", "a", "b", "aa", "ab", \dots, "bbab", \dots \}</math></span> |

# The Role of Regular Expressions

- Theorem:

- For every regular expression, there exists a nondeterministic finite-state machine that defines the same language, and vice versa.

- Q: Why is the theorem important for *scanner generation*?

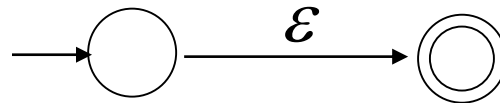
- Q: Theorem is not enough: what do we need for *automatic* scanner generation?

# Regular Expressions to NFA (1)

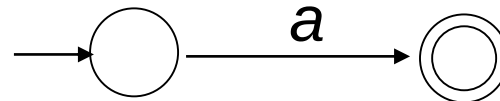
- For each kind of RE, define an NFA
  - Notation: NFA for RE  $M$



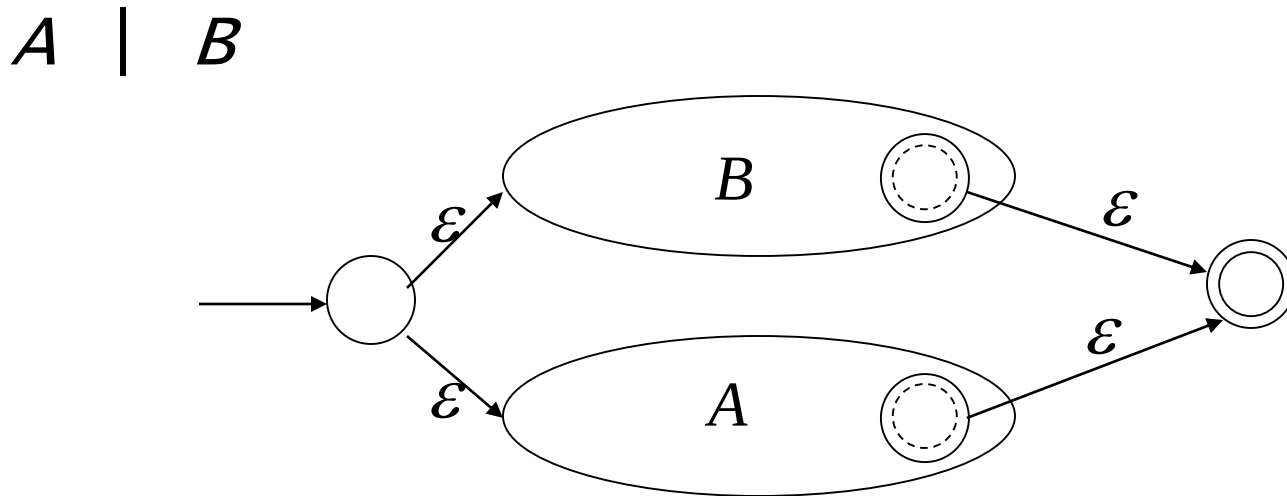
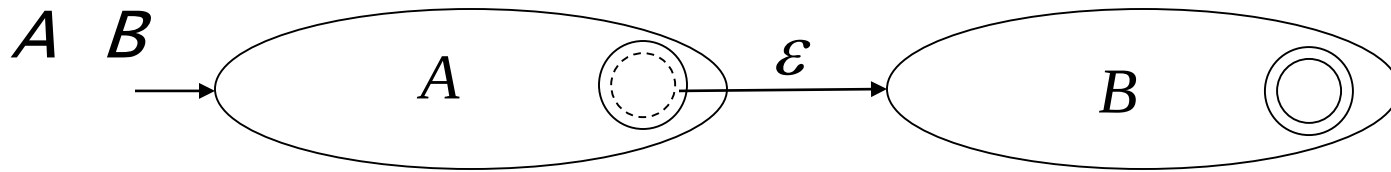
$\varepsilon$



$a$

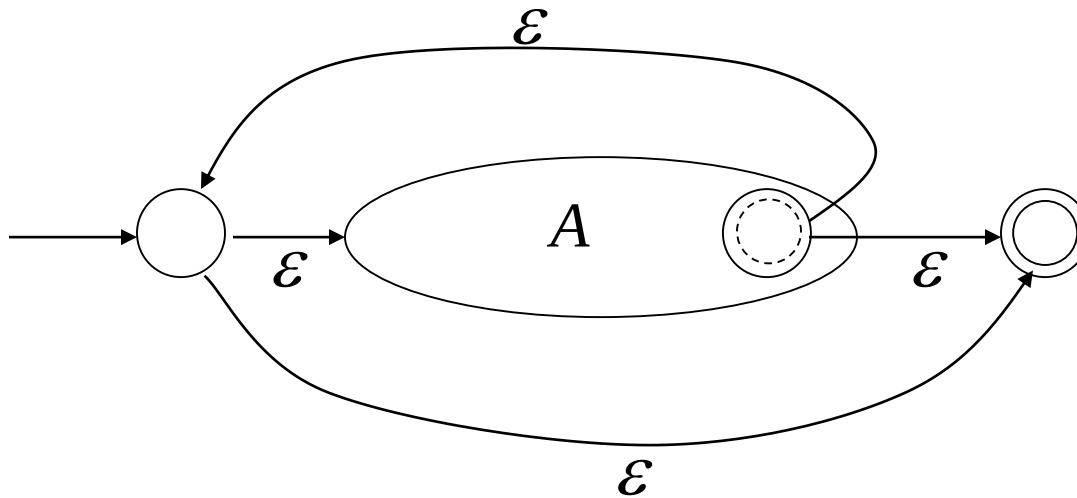


# Regular Expressions to NFA (2)



# Regular Expressions to NFA (3)

$A^*$

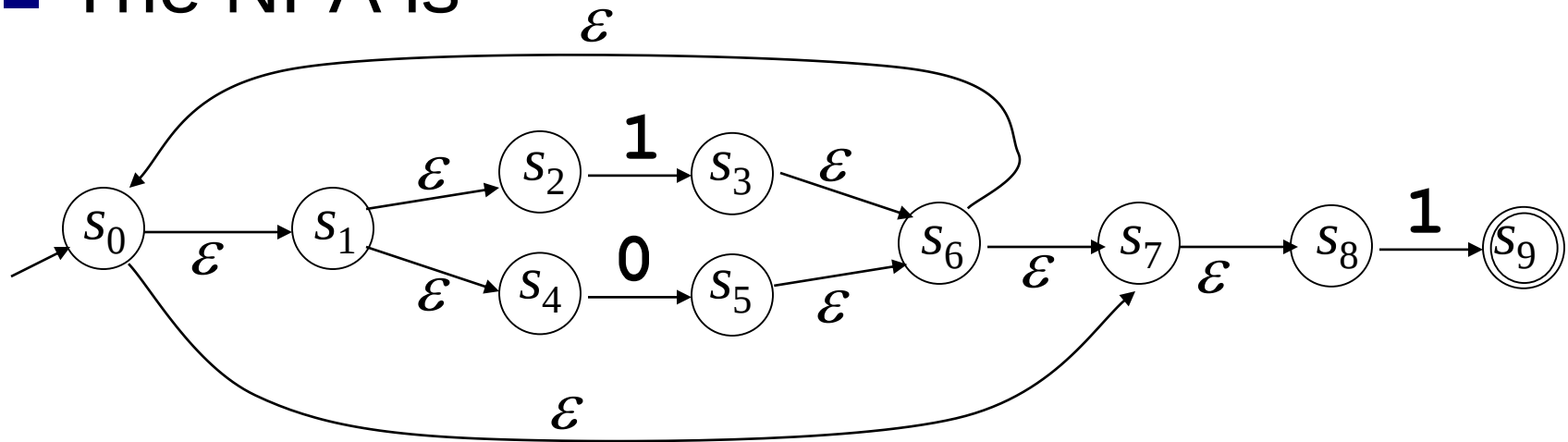


# Example : RE to NFA

- Consider the regular expression

$$(1 \mid 0)^* 1$$

- The NFA is



# Putting It All Together

- Specify regular expression for each token
  - Generate NFA and convert to DFA
- Define appropriate action for each token
  - *ignore* comments and whitespace
  - *return string* for identifier or numeric constant
  - *indicate* keyword, operator, punctuations, ...
- Associate patterns and actions
- Integrate matching of all possible patterns

# Example : Expressions

operators: `"*", "/", "+", "-"`

parentheses: `"(", ")"`

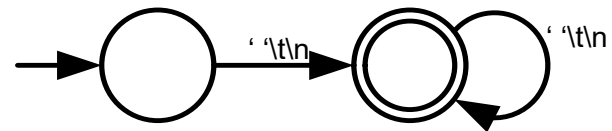
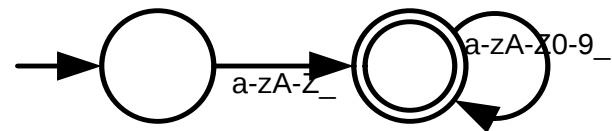
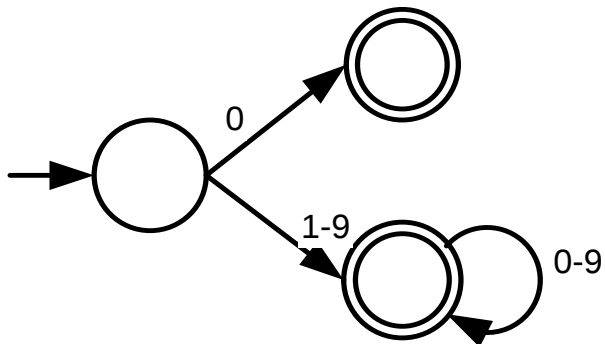
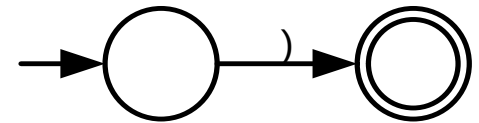
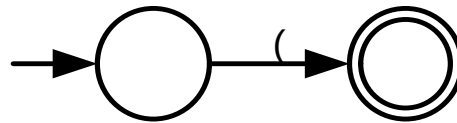
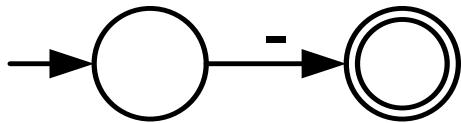
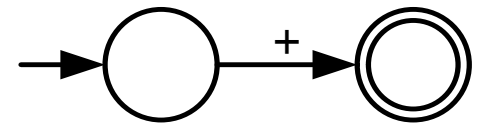
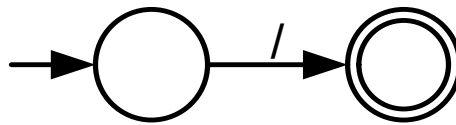
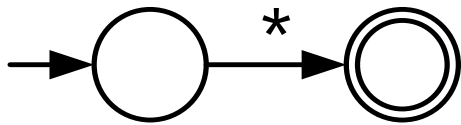
integer constants: `0 | ([1-9] [0-9] *)`

identifiers: `[a-zA-Z_] [a-zA-Z0-9_]*`

white space: `[\t\n]+`

where: `[abc] = (a | b | c)`

# Symbol DFAs



# Scanner Algorithm

Given DFA  $D_1, \dots, D_n$

```
while input is not empty do
  foreach  $i \in \{1, \dots, n\}$  do
     $s_i :=$  the longest prefix that  $D_i$  accepts;
   $k := \max\{|s_i| \mid i \in \{1, \dots, n\}\};$ 
  if  $k > 0$  then
    remove  $k$  characters from input;
     $j := \min\{i \mid |s_i| = k\};$ 
    perform the  $j^{\text{th}}$  action
  else
    move one character from input to output
    // alternatively produce scan error
```

# For You To Do

- What if more than one prefix matches a pattern?
  - Which prefix is used?
- What if a prefix matches more than one pattern?
  - Which pattern is used?
- What happens if a string matches no patterns?