# Solving the Inferential Frame Problem in the General Game Description Language

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#### **Abstract**

The Game Description Language GDL is the standard input language for general game-playing systems. While players can gain a lot of traction by an efficient inference algorithm for GDL, state-of-the-art reasoners suffer from a variant of a classical KR problem, the inferential frame problem. We present a method by which general game players can transform any given game description into a representation that solves this problem. Our experimental results demonstrate that with the help of automatically generated domain knowledge, a significant speedup can thus be obtained for the majority of the game descriptions from the AAAI competition.

#### Introduction

General Game Playing (GGP) research seeks to design systems able to understand new games and use such descriptions to play those games effectively. These systems cannot be endowed with game-specific algorithms because only at runtime they will be told the rules of a game. The general Game Description Language (GDL) (Love et al. 2006; Thielscher 2010) has been developed for this purpose and has become the standard at international GGP competition since 2005 (Genesereth, Love, and Pell 2005; Genesereth and Björnsson 2013). GDL uses formal logic to provide players with a specification of the initial game state, the possible moves and how they change the position, and the winning conditions. Players also are informed about how much time they have—the so-called STARTCLOCK—to analyse the rules and reason their way to a strategy; and how much time then to decide on every move—the PLAYCLOCK once the game has started.

For the selection of moves, two major approaches have been applied successfully in general game playing. These are depth-limited game tree search along with solution concepts like such as Minimax (Kuhlmann, Dresner, and Stone 2006; Clune 2007; Schiffel and Thielscher 2007); and guided random simulations along with statistical analysis (Finnsson and Björnsson 2008; Méhat and Cazenave 2011). For both methods the quality of play depends crucially on the number of nodes in the game tree that can be

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visited under the strict time constraints of the given PLAY-CLOCK. While ultimately a good strategy makes the difference, a lot of traction can be gained by an efficient computation of search nodes (Genesereth and Björnsson 2013).

Game trees in GGP are built by inferring the possible moves and successor states from the logical descriptions of preconditions and effects in GDL. Efficient methods exist that use tailored data structures for this purpose (Schkufza, Love, and Genesereth 2008; Waugh 2009; Kissmann and Edelkamp 2010; Saffidine and Cazenave 2011). But a recent comparative assessment of state-of-the-art reasoners has shown that still they are significantly slower than handmade, game-specific algorithms for state update, so bridging this gap is an open problem (Schiffel and Björnsson 2013).

This is a quintessentially KRR problem: A given representation of knowledge needs to be automatically turned into one that is more efficient to reason with. Specifically, reasoners for GDL face the classical *inferential frame problem* (McCarthy and Hayes 1969; Reiter 1991; Thielscher 1999): If used directly, the logical game description requires inferring all components of a successor state anew, rather than updating the current state description only by the components that change (Schiffel and Björnsson 2013).

We address this problem by developing a method for automatically transforming any given GDL description into a representation that solves the inferential frame problem. General game-playing systems apply this translation during the STARTCLOCK in order to boost the efficiency of the state update computation for their game tree search when they play the game later. The transformation consists of several steps. First, the given GDL axioms for state update are rewritten into syntactically equivalent formulas that describe the changes between successor states. Second, the resulting formulas are subjected to automatic logical simplification. Finally, and crucial for matching the efficiency of a gamespecific implementation, the representation is simplified further based on domain-specific knowledge. The latter needs to be established from the game rules through automated theorem proving (Haufe, Schiffel, and Thielscher 2012).

Our results in this paper are three-fold. We present a method by which any GDL game description is automatically turned into a representation that can be used directly to infer state updates without suffering from the inferential frame problem. We provide a formal proof of the correct-

```
1 role(x).
                                                                    11    next(cell(M, N, x)) :- does(x, mark(M, N)).
                                                                                                                           8r1
                                                                       next(cell(M,N,o)) :- does(o,mark(M,N)).
2 role(0).
                                                                                                                           8r2
3
   init (cell(1,1,b)).
                                                                    13
                                                                       next(cell(M,N,O)) :-
                                                                                                                           %r3
                                                                    14
5
   init(cell(3,3,b)).
                                                                    15
                                                                            does(P, mark(J, K)),
   init(control(x)).
                                                                            true(cell(M.N.O)).
                                                                    16
                                                                    17
                                                                            ( distinct(M, J) or distinct(N, K) ).
   legal(P, mark(M, N)) :- true(control(P)), true(cell(M, N, b)).
   legal(x, noop) :- true(control(o)).
                                                                    19
                                                                       next(control(x)) :- true(control(o)).
                                                                                                                           %r4
10 legal(o,noop) :- true(control(x)).
                                                                      next(control(o)) :- true(control(x)).
                                                                                                                           8r5
```

Figure 1: A GDL description of Tic-Tac-Toe (without the definition of termination and goalhood). Positions are encoded using the features control(P), where  $P \in \{x, o\}$ ; and cell(X, Y, Z), where  $X, Y \in \{1, 2, 3\}$  and  $Z \in \{x, o, b\}$  (with b = ``blank'').

ness of this translation, and we present experimental results obtained with a state-of-the-art reasoner, Fluxplayer (Schiffel and Thielscher 2007; Schiffel and Björnsson 2013), that demonstrate a significant efficiency gain for the majority of the GDL game descriptions from the AAAI GGP competition (Genesereth and Björnsson 2013).

Our result has implications beyond the specific game description language used for GGP. The update axioms in GDL can be viewed (Schiffel and Thielscher 2011) as general successor state axioms (SSAs), which provide the standard solution (Reiter 1991) to the frame problem—the representational aspect thereof, to be more specific—in the classical KR formalism for reasoning about actions, the Situation Calculus (McCarthy and Hayes 1969). Any standard reasoner for actions based on some form of SSAs can therefore profit from our techniques if a straightforward implementation requires to compute unchanged fluents individually.

The remainder of the paper proceeds as follows. After a brief introduction to GDL, we show how game descriptions can be rewritten into a direct representation of the changes effected by moves. We prove the correctness of the overall translation. We show how the result can be further simplified using automatically derived, game-specific knowledge. We present our experimental results and conclude.

### **Game Description Language**

GDL has been developed to formalise the rules of any finite game with complete information in such a way that the description can be automatically processed by a GGP system.

Game descriptions in GDL are sets of *normal logic program clauses* (Lloyd 1987) that may include negation and disjunction in the bodies. Especially designed for game descriptions, the language uses a few pre-defined predicates:

role(R)	R is a player			
init(F)	F holds in the initial position			
true(F)	F holds in the current position			
legal(R,M)	player R has legal move M			
does(R,M)	player R does move M			
next(F)	F holds in the next position			
terminal	the current position is terminal			
goal(R,N)	player R gets goal value N			
distinct(X,Y)	<i>X,Y</i> syntactically different terms			

In GDL it is assumed that gameplay happens synchronously,

that is, all players move simultaneously and the world changes only in response to moves.

As an example, Figure 1 shows an excerpt of a GDL description for the simple game of Tic-Tac-Toe. GDL imposes some syntactic restrictions on a set of clauses with the intention to ensure an unambiguous interpretation of the rules and finiteness of the set of derivable predicate instances (Love et al. 2006). Let it suffice to say that any valid GDL description

- must be stratified (Apt, Blair, and Walker 1987) and allowed (Lloyd and Topor 1986);
- has predicate *next* only in the head of clauses while *true* and *does* can only appear in clause bodies.

Stratified logic programs are known to admit a unique answer set (Gelfond 2008).

The semantics of a set of game rules has been informally described by a state transition system by Genesereth, Love, and Pell (2005) and later formalised as follows (Schiffel and Thielscher 2010). Let  $G \models A$  denote that atom A is true in the unique answer set of a stratified set of rules G. The players in game G are  $R = \{r : G \models role(r)\}$ . The initial state is  $\{f : G \models init(f)\}$ . A move m is legal in state  $S = \{f_1, \ldots, f_k\}$  if  $G \cup S^{true} \models legal(r, m)$ , where

$$S^{\text{true}} \stackrel{\text{def}}{=} \{ true(f_1), true(f_2), \dots, true(f_k). \}$$

A *joint move* M in state S assigns each role  $r \in R$  a legal move. The *state transition* from S via M is defined by

$$\{f: G \cup S^{\text{true}} \cup M^{\text{does}} \models \textit{next}(f)\}$$
 (1)

Here,  $S^{\text{true}}$  is as above and

$$M^{\text{does}} \stackrel{\text{def}}{=} \{ does(r_1, m_1)., \ldots, does(r_n, m_n). \}$$

assuming that joint move M assigns  $m_i$  to player  $r_i$ . Finally, a terminal state is any S such that  $G \cup S^{\text{true}} \models \text{terminal}$ ; and a goal value for player  $r \in R$  in state S is any v for which  $G \cup S^{\text{true}} \models \text{goal}(r,v)$  holds.

#### **Solving the Inferential Frame Problem in GDL**

The inferential frame problem in GDL is the problem of having to compute anew all the elements of a state that persist

<sup>&</sup>lt;sup>1</sup>A word on the syntax: We use a Prolog-style notation for GDL rules as we find this more readable than the usual prefix notation used at competitions. Variables are denoted by uppercase letters.

after a move. For example, in Tic-Tac-Toe when a player marks a cell then all the other cells remain unchanged. In GDL this persistence has to be represented explicitly by a frame rule, as r3 in Fig. 1. Hence, when a reasoner updates a state it has to recompute the values of all the cells that persist. In contrast, consider the following rule:

```
 \textbf{fnext} \, (\texttt{cell} \, (\texttt{M}, \texttt{N}, \texttt{O}) \,) := \, \textbf{does} \, (\texttt{P}, \texttt{mark} \, (\texttt{M}, \texttt{N}) \,) \,, \\ \textbf{true} \, (\texttt{cell} \, (\texttt{M}, \texttt{N}, \texttt{O}) \,) \,.
```

where fnext/1 is a new predicate to represent that a true element changes to false in the next state. Intuitively, this fnext rule says that a cell loses its previous mark when it gets marked by a player. In contrast to frame rule r3, which has to be executed once for every individual cell that persists, the fnext rule only has to be executed once per turn.

Our solution to the inferential frame problem in GDL is to translate frame rules such as r3 into *fnext* rules and then use the latter instead. In this way, rather than having to compute everything that persists, the reasoner will compute everything that changes to false. In most of the domains there are far less changes to false than persisting state features, so we expect an improvement in the performance of the reasoner.

#### **Preliminaries**

Let  $\phi = \{v_1/t_1, \dots, v_n/t_n\}$ .  $\phi$  is said to be a substitution when each  $v_i$  is a variable and each  $t_i$  is a term, and for no distinct i and j is  $v_i$  the same as  $v_j$ . We denote by  $Eq(\phi)$  the formula  $\bigwedge_{v_i/t_i \in \phi} v_i = t_i$ . Let l be a literal and let  $\phi = \{v_1/t_1, \dots, v_n/t_n\}$  be a substitution. The instantiation of l by  $\phi$ , written  $l\phi$ , is formed by replacing every occurrence of  $v_i$  in l by  $t_i$ . The instantiation of a set of literals L by  $\phi$ , written  $L\phi$ , is the set of the instantiations of the literals of L by  $\phi$ . Atom a subsumes atom b, or  $a \succeq b$ , if there is a substitution  $\phi$  such that  $a\phi = b$ . For sets of atoms A and B, we say that A subsumes B, or  $A \succeq B$ , if there is a substitution  $\phi$  such that  $A\phi \supseteq B$ .

We consider logic programming notation as an alternative to first order logic notation, interpreting the symbol  $\leftarrow$  as logical implication, every comma as  $\land$ , every or as  $\lor$  and every not as ¬, and assuming all free variables are universally quantified from the outside. We identify a set of formulas with the conjunction of its elements, and sometimes we omit the curly braces among the elements of a set. For a rule r, by  $head_r$  we refer to the atom in the head, by  $body_r$ we refer to the set of conjuncts in the body, and by  $does_r$  we refer to the set of positive literals of predicate does/2 in the body. A next rule is a rule whose head is an atom of predicate next/1, and by  $G_{next}$  we refer to the next rules of a GDL description G. An *fnext rule* is a rule whose head is an atom of predicate  $f_{next}/1$ . We assume that  $f_{next}/1$  does not appear anywhere in a given GDL description. Let r be a next rule with head next(f), then we say that r is a frame rule if true(f) belongs to the body of the rule. In this case we denote by  $cond_r$  the condition  $body_r \setminus (\{true(f)\} \cup does_r)$ and we may write r as:

$$next(f) \leftarrow true(f) \land does_r \land cond_r$$

For example, in the Tic-Tac-Toe description, the next rules are  $r_1, r_2, \ldots, r_5$  (cf. the labels in Fig. 1);  $r_3$  is the unique

frame rule;  $does_{r_3}$  is  $\{does(P, mark(J, K))\}$ ; and  $cond_{r_3}$  is  $\{M \neq J \lor N \neq K\}$ . Let P be a set of predicates and A a set of ground atoms of predicates from P, the closed world assumption (Reiter 1978) over predicates P in A, written  $CWA_P(A)$ , is the set of formulas  $p(\vec{x}) \leftrightarrow \bigvee_{p(\vec{t}) \in A} \vec{x} = \vec{t}$  for every  $p \in P$ , where  $\vec{x}$  is a tuple of distinct variables,  $\vec{t}$  is a tuple of ground terms and  $\vec{x} = \vec{t}$  is interpreted as usual. We may define the state transition from a state S via a joint move M as:

$$\{f: CWA_P(A) \cup G_{next} \models_{FOL} next(f)\}$$
 (2)

where A is the unique answer set of the program  $G' = (G \setminus G_{next}) \cup S^{\text{true}} \cup M^{\text{does}}, P$  are the predicates that appear in G', and  $\models_{FOL}$  is the entailment relationship in first-order logic under the unique names assumption. Using the fact that predicate next/1 does not appear in G', the following theorem is easy to prove.

**Theorem 1** *The definitions of the state transitions (1) and (2) are equivalent.* 

#### The Translation

We describe the translation for a GDL description G with a set of players R. We say that f is a fluent of G if  $f \in S$  for some state S of G. For the simple case where G is ground and there is a single player  $p \in R$ , for every fluent f and every move m we have the *fnext* rule:

$$\mathit{fnext}(f) \leftarrow true(f) \land does(p,m) \land \bigwedge_{r \in \mathcal{F}\!r(f,m)} \neg cond_r$$

where  $\mathcal{F}r(f,m)$  is the set of frame rules r with head next(f) and  $does_r \subseteq \{does(p,m)\}$ . Intuitively, the rule says that f changes to false by move m if none of the conditions hold for f to persist. For this simple case the translation is straightforward: For every fluent f and every move f we replace the frame rules from f by the new f rules, and we modify the state transition definition so that f belongs to a successor state if either f is entailed or f is true in the previous state and f f is not entailed.

The general case requires two generalizations. First, the translation is defined for possibly non ground atoms a of predicate next/1. For any such atom a the frame rules in G, written  $\mathcal{F}r_G(a)$ , are the set of frame rules  $r \in G$  such that  $a \succeq head_r$ . For example,  $r_3$  is a frame rule for atom next(cell(X,Y,Z)) but not for next(cell(X,Y,b)).

Second, the translation is defined for a set of possibly non ground atoms of predicate does/2. For this we introduce the concept of a general joint move. We say that M is a joint move of G if it is a joint move in some state S of G. A general joint move  $\mathcal M$  of G is a set of |R| atoms of predicate does/2 such that the first terms of two distinct elements of  $\mathcal M$  are different. Intuitively, a general joint move is a set of does/2 atoms that can be instantiated to a joint move. Every joint move M of G is also a general joint move of G, and the set  $\bigcup_{1\leq i\leq |R|}\{does(P_i,A_i)\}$  is a general joint move of any G with |R| players. For the Tic-Tac-Toe description,

```
\mathcal{M}_1 = \{does(x, noop), does(o, noop)\}

\mathcal{M}_2 = \{does(x, noop), does(o, mark(A, B))\}

\mathcal{M}_3 = \{does(P_1, noop), does(P_2, mark(A, B))\}
```

are some other general joint moves. For a general joint move  $\mathcal{M}$ , by  $\mathcal{I}_{\mathcal{M}}$  we denote the set of inequalities  $p_i \neq p_j$  for every two distinct atoms  $does(p_i, m_i)$ ,  $does(p_j, m_j) \in \mathcal{M}$ . For example,  $\mathcal{I}_{\mathcal{M}_1}$  and  $\mathcal{I}_{\mathcal{M}_2}$  are  $\{x \neq o\}$  and  $\mathcal{I}_{\mathcal{M}_3}$  is  $\{P_1 \neq P_2\}$ .

#### Translation for an atom and a general joint move

We first define the translation for an atom a of predicate next/1 and a general joint move  $\mathcal{M}$  of G. We assume that a and  $\mathcal{M}$  have different variables that do not appear in G.

The set of unifiers of a rule  $r \in \mathcal{F}r_G(a)$  with a and  $\mathcal{M}$ , written  $\mathcal{U}_r(a,\mathcal{M})$ , is the set of substitutions  $\phi$  such that  $(head_r \cup does_r)\phi \subseteq (a \cup \mathcal{M})\phi$ .

For example,  $\mathcal{U}_{r_3}(next(cell(X,Y,Z)),\mathcal{M}_1)=\emptyset$ , while  $\mathcal{U}_{r_3}(next(cell(X,Y,Z)),\mathcal{M}_2)$  has many elements, including  $\{X/M,Y/N,Z/O,A/J,B/K,P/o\}$ .

For a rule  $r \in \mathcal{F}r_G(a)$ , if  $\mathcal{M}$  subsumes  $M^{\text{does}}$  for a joint move M, then we may rewrite r as  $r(a, \mathcal{M})$ :

The set  $\mathcal{I}_{\mathcal{M}}$  is added to guarantee that if the body holds then  $\mathcal{M}$  is instantiated to a joint move. Formally, we have the following proposition.

**Proposition 1** Let a,  $\mathcal{M}$  and r be defined as above. For any joint move M in a state S such that  $\mathcal{M} \succ M^{\text{does}}$ , the sets

$$\{f: CWA_P(A) \cup r \models_{FOL} next(f)\}$$
 (3)

and 
$$\{f: CWA_P(A) \cup r(a, \mathcal{M}) \models_{FOL} next(f)\}$$
 (4) are the same (A and P are as in (2)).

*Proof*: ( $\Rightarrow$ ) Let  $g \in (3)$ , we prove that  $g \in (4)$ . If  $g \in (3)$  then there is a substitution  $\alpha$  such that  $\alpha$  only mentions variables in r,  $head_r\alpha$  and  $body_r\alpha$  are ground,  $CWA_P(A) \models_{FOL} body_r \alpha$  and  $head_r \alpha$  is next(g). Given that  $r \in \mathcal{F}r_G(a)$  there is a substitution  $\beta$  that only mentions variables in a such that  $a\beta = head_r$ . Also, given that  $\mathcal{M} \succeq$  $M^{\mathrm{does}}$  there is a substitution  $\gamma$  that only mentions variables in  $\mathcal M$  such that  $\mathcal M\gamma=M^{\mathrm{does}}.$  Let  $\delta$  be the composition  $\beta \gamma \alpha$  and let  $head_r$  be of the form next(h). We show that all the elements of  $body_{r(a,\mathcal{M})}\delta$  are entailed by  $CWA_P(A)$ :  $true(f)\delta$  is entailed because  $true(f)\beta = true(h)$  and  $true(h)\alpha$  is entailed by  $CWA_P(A)$ ,  $(\mathcal{M} \wedge \mathcal{I}_{\mathcal{M}})\delta$  is entailed because  $\mathcal{M}\gamma$  is equal to  $M^{\text{does}}$ , which is entailed by  $CWA_P(A)$ ,  $cond_r\delta$  is entailed because  $cond_r\alpha$  is entailed by  $\mathit{CWA}_P(A)$ , and for the disjunction  $\bigvee_{\phi \in \mathcal{U}_r(a,\mathcal{M})} Eq(\phi)$ we have that  $\delta \in \mathcal{U}_r(a, \mathcal{M})$  and  $Eq(\delta)\delta$  is a tautology. Finally, given that  $a\beta = head_r$  and  $head_r\alpha$  is next(g)we have that  $a\delta$  is next(g), and given that the elements of  $body_{r(a,\mathcal{M})}\delta$  are entailed by  $CWA_P(A)$  we have that next(g)is entailed by  $CWA_P(A) \cup r(a, \mathcal{M})$  and  $g \in (4)$ .

$$(\Leftarrow)$$
 Similar to the other direction.

In  $r(a, \mathcal{M})$  we are considering all substitutions  $\phi \in \mathcal{U}_r(a, \mathcal{M})$ , but we only need to consider the most general ones. For this, we define a selection of unifiers of r with a and  $\mathcal{M}$  as a set  $S \subseteq \mathcal{U}_r(a, \mathcal{M})$  such that: (1) for every  $\alpha \in \mathcal{U}_r(a, \mathcal{M})$ , there exists  $\beta \in S$  such that  $(head_r \cup does_r)\beta \succeq$ 

 $(head_r \cup does_r)\alpha$ , and (2) for every  $\alpha, \beta \in S$ , if  $\alpha \neq \beta$ , then  $(head_r \cup does_r)\alpha \not\succeq (head_r \cup does_r)\beta$ . The selections of most general unifiers are unique up to variable renaming, so to simplify the presentation we abuse notation by referring to the selection of most general unifiers, denoted by  $\mathcal{U}_r^*(a,\mathcal{M})$ . Then we may define  $r^*(a,\mathcal{M})$  as we did for  $r(a,\mathcal{M})$  but using  $\mathcal{U}_r^*(a,\mathcal{M})$  instead of  $\mathcal{U}_r(a,\mathcal{M})$ , and Proposition 1 still holds if we use  $r^*(a,\mathcal{M})$  in (4) instead of  $r(a,\mathcal{M})$ . In the Tic-Tac-Toe description,  $r_3^*(next(cell(X,Y,Z)),\mathcal{M}_2)$  is:

$$\begin{aligned} & \mathit{next}(cell(X,Y,Z)) \leftarrow \mathit{true}(cell(X,Y,Z)) \land \\ & does(x,noop) \land does(o,mark(A,B)) \land x \neq o \land \\ & (M \neq J \lor N \neq K) \land \\ & (X = M \land Y = N \land Z = O \land A = J \land B = K \land P = o) \end{aligned}$$

The set of rules  $\{r^*(a,\mathcal{M}) \mid r \in \mathcal{F}r_G(a)\}$  represents the persistence of the fluents g such that  $a \succeq next(g)$  when a joint move M with  $\mathcal{M} \succeq M^{\text{does}}$  is performed. Then we may define the translation of a for  $\mathcal{M}$  in G, written  $\mathcal{T}_G(a,\mathcal{M})$ , as the first-order *fnext* rule:

$$\begin{array}{c} \mathit{fnext}(f) \leftarrow \mathit{true}(f) \land \mathcal{M} \land \mathcal{I}_{\mathcal{M}} \land \\ \left( \bigwedge_{r \in \mathcal{F}r_G(a)} \bigwedge_{\phi \in \mathcal{U}^*_r(a,\mathcal{M})} \neg \exists \vec{x} (cond_r \land Eq(\phi)) \right) \\ \end{array}$$

where a is next(f) and  $\vec{x}$  are the variables appearing in r. We add the existential quantifier inside the rule because we have to make sure that for no possible substitution of the variables the conditions hold. Intuitively, the rule says that an instance of f changes to false after doing an instance of  $\mathcal{M}$  if none of the conditions hold for f to persist. This generalizes the simple case, where all the elements are ground and  $\mathcal{M}$  is a singleton set. In the Tic-Tac-Toe description,  $\mathcal{T}_G(next(cell(X,Y,Z)),\mathcal{M}_2)$  is:

$$\begin{split} & \textit{fnext}(cell(X,Y,Z)) \leftarrow \textit{true}(cell(X,Y,Z)) \land \\ & \textit{does}(x,noop) \land \textit{does}(o,mark(A,B)) \land x \neq o \land \\ & \neg \exists MJNKOP \\ & \big( (M \neq J \lor N \neq K) \land \\ & X = M \land Y = N \land Z = O \land A = J \land B = K \land P = o \big) \end{split}$$

The following proposition states formally the role of  $\mathcal{T}_G(a,\mathcal{M})$ .

**Proposition 2** Let a and  $\mathcal{M}$  be defined as above. For any joint move M in a state S such that  $\mathcal{M} \succeq M^{\text{does}}$ , the sets

$$\{f: CWA_P(A) \cup \mathcal{F}r_G(a) \models_{FOL} next(f)\}$$
 (5)

and

$$\begin{cases} f: a \succeq \textit{next}(f), f \in S^{\textit{true}} \textit{ and} \\ \textit{CWA}_P(A) \cup \mathcal{T}_G(a, \mathcal{M}) \not\models_{FOL} \textit{fnext}(f) \end{cases}$$
 (6)

are the same (A and P are as in (2)).

*Proof Sketch:* It holds that  $f \in (5)$  iff there is a rule  $r \in \mathcal{F}r_G(a)$  such that  $CWA_P(A) \cup r \models_{FOL} next(f)$  iff (by Proposition 1) there is a rule  $r \in \mathcal{F}r_G(a)$  such that  $CWA_P(A) \cup r(a,\mathcal{M}) \models_{FOL} next(f)$  iff  $a \succeq next(f)$ ,  $f \in S^{\text{true}}$  and  $CWA_P(A) \cup \mathcal{T}_G(a,\mathcal{M}) \not\models_{FOL} fnext(f)$  iff  $f \in (6)$ .

### The complete translation

To replace the frame rules from the GDL description we have to make sure that the new *fnext* rules cover any possible move of the game. For this we introduce the concept of a *move covering*, a set of general joint moves such that for every joint move M in a state that is reachable from the initial state there is an element of the set that subsumes  $M^{\text{does}}$ . For example, the singleton set  $\{\bigcup_{1 \leq i \leq |R|} \{does(P_i, A_i)\}\}$  is a generic move covering for any game G with |R| players. Another move covering for the Tic-Tac-Toe description is

$$C_1 = \{ \{ does(x, noop), does(o, mark(A, B)) \}, \\ \{ does(o, noop), does(x, mark(A, B)) \} \}$$
 (7)

Now given an atom a of predicate next/1 and a move covering  $\mathcal C$  we can replace the frame rules  $\mathcal Fr_G(a)$  by the fnext rules  $\bigcup_{\mathcal M\in\mathcal C}\mathcal T_G(a,\mathcal M)$ . For every fluent f such that  $a\succeq next(f)$  and every joint move M in a reachable state S there is an  $\mathcal M\in\mathcal C$  that subsumes  $M^{\mathrm{does}}$ . Then by Proposition 2, next(f) is entailed by a frame rule if and only if fnext(f) is not entailed by the fnext rules, and we can redefine the state transition just like in the simple case.

In order to translate many atoms at the same time we define a *translation basis* as a set  $\mathcal{X} = \{\langle a_1, \mathcal{C}_1 \rangle, \dots, \langle a_n, \mathcal{C}_n \rangle\}$  where each  $a_i$  is an atom of predicate next/1 and each  $\mathcal{C}_i$  is a move covering. In the Tic-Tac-Toe description, for example,

$$\mathcal{X}_1 = \{ \langle next(cell(X, Y, Z)), \mathcal{C}_1 \rangle, \langle next(control(X)), \mathcal{C}_1 \rangle \}$$

is a translation basis, where  $C_1$  is as in (7). The translation of  $\mathcal{X}$  in G, written  $G^{\mathcal{X}}$ , is

$$\bigcup_{\langle a,\mathcal{C}\rangle\in\mathcal{X}} \big(\bigcup_{\mathcal{M}\in\mathcal{C}} \mathcal{T}_G(a,\mathcal{M})\big)$$

In the Tic-Tac-Toe example, after some logical simplifications we obtain that  $G^{\chi_1}$  is the following set of rules:

Let  $\mathcal{F}^{\mathcal{X}}$  be the set  $\{f \mid f \text{ is a fluent and for some } \langle a, \mathcal{C} \rangle \in \mathcal{X}, a \succeq next(f)\}$  of fluents that are translated in  $G^{\mathcal{X}}$ , and let  $\mathcal{F}r_G^{\mathcal{X}}$  be the set  $\bigcup_{\langle a,\mathcal{C} \rangle \in \mathcal{X}} \mathcal{F}r_G(a)$  of the frame rules in G that have been translated in  $G^{\mathcal{X}}$ . We define the  $\mathcal{X}$ -translation state transition from a state S via a joint move M as:

$$\{ f : CWA_P(A) \cup (G_{next} \setminus \mathcal{F}r_G^{\mathcal{X}}) \models_{FOL} next(f) \} \cup \\ \{ f \in \mathcal{F}^{\mathcal{X}} \cap S^{\text{true}} : CWA_P(A) \cup G^{\mathcal{X}} \not\models_{FOL} fnext(f) \}$$
 (8)

**Theorem 2** The definitions of the state transitions (1), (2) and (8) are equivalent.

*Proof Sketch:* Given Theorem 1 it suffices to prove that the update transitions (2) and (8) are equivalent. It holds that  $f \in (2)$  iff either (i)  $CWA_P(A) \cup (G_{next} \setminus \mathcal{F}r_G^{\mathcal{X}}) \models_{FOL} next(f)$  or  $CWA_P(A) \cup \mathcal{F}r_G^{\mathcal{X}} \models_{FOL} next(f)$  iff either (i) or for some  $\langle a, \mathcal{C} \rangle \in \mathcal{X}$ ,  $CWA_P(A) \cup \mathcal{F}r_G(a) \models_{FOL} next(f)$ 

iff either (i) or (by Proposition 2) for some  $\langle a, \mathcal{C} \rangle \in \mathcal{X}$  it holds that  $a \succeq next(f)$ , and also  $f \in S^{\text{true}}$  and for every  $\langle a, \mathcal{C} \rangle \in \mathcal{X}$  such that  $a \succeq next(f)$  and every  $\mathcal{M} \in \mathcal{C}$  such that  $\mathcal{M} \succeq M^{\text{does}}$  it is the case that that  $CWA_P(A) \cup \mathcal{T}_G(a,\mathcal{M}) \not\models fnext(f)$  iff either (i) or  $f \in \mathcal{F}^{\mathcal{X}}$ ,  $f \in S^{\text{true}}$  and  $CWA_P(A) \cup G^{\mathcal{X}} \not\models_{FOL} fnext(f)$  iff  $f \in (8)$ .

## **Empirical Evaluation**

#### **Implementing the Translation**

The translation described in the previous section is parametric over a translation basis  $\mathcal{X}$ . Early experimentation indicated that the generic singleton move covering could be improved by partially grounding the role and action terms.

In a preliminary step, we perform a simple reachability analysis to compute a superset of the domain of the *next* and *does* predicates. This allows us to identify the roles R in the game, as well as the fluent names  $\mathcal{F}$  and for each role r, the action names  $\mathcal{A}_r$  for that role. We can then define the *direct* move covering  $\mathcal{C}_D = \{\bigcup_{r \in R} \{does(r, m_r)\} : m_1 \in A_1, \ldots, m_{|R|} \in A_{|R|}\}$ . In Tic-Tac-Toe, we obtain the roles  $\{x, o\}$ , the fluent names  $\{control, cell\}$ , and the same action names  $\{mark, noop\}$  for both roles.

```
\mathcal{C}_D = \{ \{ does(x, noop), does(o, noop) \}, \\ \{ does(x, noop), does(o, mark(A, B)) \}, \\ \{ does(x, mark(A, B)), does(o, noop) \}, \\ \{ does(x, mark(A, B)), does(o, mark(C, D)) \} \}
```

The direct move covering sometimes contains general joint moves that can never appear in the reachable states of the game. It is possible to use the theorem proving technique described by Haufe, Schiffel, and Thielscher (2012) to derive automatically whether an instance of a given general joint moves can ever occur in a reachable state. Never occurring general joint moves can safely be removed from the covering. We call  $\mathcal{C}_P$  the *pruned* move covering resulting from  $\mathcal{C}_D$  after pruning provably impossible general joint moves. In Tic-Tac-Toe, we obtain  $\mathcal{C}_P = \mathcal{C}_1$  as in (7).

The corresponding *direct* translation basis is  $\mathcal{X}_D = \{\langle next(f), \mathcal{C}_D \rangle : f \in \mathcal{F} \}$ , and the *pruned* translation basis is  $\mathcal{X}_P = \{\langle next(f), \mathcal{C}_P \rangle, f \in \mathcal{F} \}$ .

The rest of the implementation follows the first order logic description provided in the previous section to obtain an encoding in a GDL-like form. The only difference is that since GDL does not allow direct universal quantification, we need to introduce auxiliary predicates to capture the universally quantified variables.

#### **Experimental Results**

We implemented the two described translations to generate alternative game rule encodings and we used the FluxPlayer system to process them. The FluxPlayer system is based on ECLiPSe Prolog and has been participating in GGP competitions since 2006.

We can now proceed to measure whether the proposed translations improve the performance of a game engine based on the FluxPlayer system. In its standard operational

Table 1: Time needed for a minimax search up to depth d using various encodings, in seconds.

using various cheodin		i seconds.		
Game G	d	k-states	0	$\mathcal{X}_D$ $\mathcal{X}_P$
amazons	1	2.13	0.10	0.10 0.08
battle	1	2.31	0.82	0.98
beatmania	6	598	20.5	21.3
blocks	14	1240	30.3	24.7
brawl	3	55.5	36.2	15.1 <b>13.9</b>
breakthrough	4	268	66.4	26.2 <b>21.5</b>
bunk_t	3	259	22.3	39.8 <b>15.1</b>
buttons	13	2390	56.9	88.9
checkers	5	26.9	21.0	23.2 <b>13.7</b>
chinesecheckers1	6	134	33.2	<b>7.9</b> 7
chinesecheckers2	6	139	42.0	11.7 <b>10.7</b>
chinesecheckers3	6	139	50.5	21.9 <b>12.6</b>
chinesecheckers4	6	53.2	22.3	30.1 <b>11.7</b>
chinesecheckers6	6	128	78.0	519 <b>23.5</b>
chinesecheckers6		110		
-simultaneous	1	118	37.2	193
chomp	3	65.6	16.2	9.50 <b>9.19</b>
crisscross	9	139	25.5	18.6 <b>15.8</b>
doubletictactoe	3	259	22.3	41.0
dup-statelarge	9	350	38.0	38.6
dup-statemedium	10	1400	76.9	70.5
firefighter	5	1190	10.8	12.9
hanoi	13	1040	40.5	38.0
knightstour	10	2690	72.5	101
knightthrough	3	65.2	13.9	4.56 <b>4.10</b>
max_knights	2	4.10	2.18	7.59
minichess	8	188	20.4	40.5 24.7
nim1	8	740	47.5	50.9 <b>46.9</b>
nim2	5	997	28.0	35.7 29.7
nim3	3	158	3.15	4.51 3.54
nim4	3	169	3.44	4.81 3.85
numbertictactoe	2	104	3.68	3.08 <b>2.50</b>
othello-comp2007	6	20.3	57.9	57.8
othellosuicide	6	20.3	58.0	57.7
pancakes6	8	2020	24.8	41.7
pawn_whopping	5	234	24.0	25.7
pawntoqueen	7	5.28	58.4	34.9 <b>34.7</b>
pentago_2008	5	2830	62.8	125 81.8
point_grab	3	1010	18.0	193
racer	1	2.71	0.26	0.36
racetrackcorridor	3	350	84.8	295
roshambo2	5	1120	18.6	235
ruledepthexp	13	16.4	37.6	39.1
ruledepthlinear	20	2100	33.0	35.0
sheep_and_wolf	7	31.1	19.5	7.21 <b>5.16</b>
skirmish	5	42.4	26.6	10.5 9.58
statespacelarge	9	350	26.6	23.9
statespacemedium	10	1400	89.2	74.3
sum15	8	624	36.2	29.8 <b>26.1</b>
tictactoe	9	986	56.6	48.9 <b>43.7</b>
tictactoeserial	6	86.4	54.4	47.8 <b>40.4</b>
tictictoe	3	143	18.5	12.6
wallmaze	6	289	88.6	144
				- 1 1

mode, FluxPlayer uses the underlying Prolog implementation and Prolog's assert and retract mechanism to maintain the set of fluent instances holding in the current game state. Measuring engine speed in GGP is typically done by selecting games from previous GGP competitions and running the game engine related part of standard search algorithms. Following recent work by Schiffel and Björnsson (2013), we use the time needed for a naive minimax search to estimate the raw performance. The benchmark domains have been used in international or local GGP competitions and can be found online.<sup>2</sup>

We translate each game under consideration using the direct and the pruned translation bases. The time needed for the transformation between the classical and proposed encodings falls under ten second. The translation is performed once per game and all GGP competitions so far use much longer STARTCLOCK and PLAYCLOCK, so we can disregard the transformation time from our considerations.

Table 1 aggregates the results. For each game G under consideration, d is the maximal depth reachable in an iterative deepening minimax search within 3 minutes using the classical state transition. We then measure the time (in seconds) needed to perform a full minimax search up to d with the proposed encodings: the original state transition  $\mathcal{O}$ , the direct translation  $\mathcal{X}_D$ , and the pruned translation  $\mathcal{X}_P$ .

As an additional precaution, we output with each encoding the number of visited states in the minimax search. Asserting that all encodings induce the same number of visited states for a given search depth increases the confidence in the correctness of the implementation. The *k-states* column indicates the number of states (in thousands) involved in the search.

#### **Discussion and Conclusion**

When the theorem proving approach cannot rule out any general joint move, the  $\mathcal{X}_D$  and  $\mathcal{X}_P$  encodings are identical. This happens mostly in games with simultaneous moves, in particular in single-agent problems.

We can see that in an important fraction of the domains, the pruned frame encoding  $\mathcal{X}_P$  leads to an engine at least twice as fast as the original encoding. Expectedly, using a pruned action covering always improves the performance over the naive action covering. Nevertheless, the naive move covering encoding already provides a notable improvement over the original encoding in a majority of the games.

The existence of domains for which our translation provides no improvement should not deter from its adoption, in particular from a portfolio perspective. Indeed, a general game player can benchmark the original and the translated encodings during the set-up time, and use the faster one in the PLAYCLOCK.

We have shown that our translation could indeed improve the performance of reasoners in General Game Playing. While our presentation and evaluation were focussed on the Game Description Language, our approach can be applied to other successor state axioms-based action formalisms.

<sup>&</sup>lt;sup>2</sup>http://games.ggp.org

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