Visualizing Answer Set Programming

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Abstract

A distinguishing feature of Answer Set Programming (ASP) is its declarativity, decoupling problem representations from problem solving algorithms. However, this strict separation should not lead to viewing the solving process as a magic black box refusing any insights into how the problem is solved.

My thesis project aims at creating visualization tools suitable to enhance the transparency of ASP systems. The first part presented here focuses on the solving of propositional ASP programs and consists of a flexible data logger protocoling relevant events occurring during ASP solving as well as a visualization back-end offering various views on both the underlying problem structure and the solving process.

The presented system allows to re-connect the solving process with the original problem specification and thus to reveal how the original problem is actually solved. However, it is currently aimed at ASP developers and contains no information from the grounding process that transforms the first-order specification into the propositional encoding given to the solver. My current research focus is on incorporating information from the grounding phase to make the tools usable for users who usually do not necessarily have the same level of experience with ASP.

1 Introduction

Answer Set Programming (ASP; (Baral 2003)) is an approach to declarative problem solving that combines a rich yet simple modeling language with high-performance solving capacities. A distinguishing feature of ASP lies in its high declarativity, strictly separating a problem’s representation from the algorithms used for solving it. As a matter of fact, this brings about new challenges given that traditional software engineering techniques relying on the connection between program specification and execution are inapplicable. A prominent example is the failure of procedural techniques like tracing. This separation is even enlarged during ASP’s solving process transforming first-order programs into a propositional format. In this way, the combination of a few first-order rules with a large set of facts may lead to a vast set of propositional rules. Furthermore, modern conflict-driven ASP solvers turn the resulting set of rules into an even larger set of Boolean constraints being subject to solving.

However, this strict separation should not lead to viewing the solving process as a magic black box refusing any insights into how the problem is solved. We address this by greatly enhancing the transparency of the solving process. We accomplish this by a two-fold approach. At first, we provide a flexible data logger protocling relevant events occurring during ASP solving. The recorded information can subsequently be used in various ways by back-ends of choice. With such data at hand, we then furnish a visualization back-end offering various views on the underlying problem structure as well as the solving process over time. Together both tools allow us to re-connect the solving process with the original problem specification and thus to reveal how the original problem is actually solved. We have implemented our data logger as an extension to the
conflict-driven constraint learning ASP solver clasp (Gebser et al. 2012). The resulting system, called clavis, is easily configurable and allows for monitoring all (single-threaded) configurations of clasp. The issuing data is provided as an event series reflecting the solving process, and stored as a queryable database. This event series serves as input to our solver-independent visualization tool insight, providing various structural and temporal perspectives on the solving process. The structural views rely on graphs for projecting different forms of variable dependencies, like occurrences in the same program or conflict constraint. To provide enriched node information, insight exploits the ASP solver’s symbol table to link solver variables to ground atoms of the original problem specification. This is accompanied with a simple query language that allows us to restrict the projection to variables satisfying a given query. While the structural perspectives come with alternative variable-specific values aggregated over the solving process, the different temporal views aim at capturing the dynamics of the solving process. Hence, they focus on indicative algorithmic figures, like the development of the conflict or decision level over time. Such developments are provided as two-dimensional plots. Within these plots particular event segments can be selected to induce in turn a structural perspectives restricted to the aggregated values of the period in focus.

2 Background

We assume some familiarity with ASP, its semantics as well as its basic language constructs. A comprehensive treatment of ASP can be found in (Baral 2003).

Once a problem is modeled as a (first-order) logic program, ASP solving proceeds in two steps. First, a grounder generates a finite propositional representation of the input program. After that, a solver computes the stable models of the propositional program. The resulting stable models represent the solutions to the original problem.

For computing the stable models of a logic program by means of modern Boolean constraint technology, the problem must be expressed in terms of Boolean constraints. For this, we rely on nogoods (Dechter 2003) representing invalid partial assignments. A solution for a set of nogoods is then a total (Boolean) assignment excluding all nogoods. While clauses can be directly mapped into nogoods, logic programs are subject to a more complex translation, often involving the introduction of auxiliary (propositional) variables. For instance, by abbreviating elementary Boolean assignments \( x \mapsto T \) and \( x \mapsto F \) by signed literals of form \( Tx \) and \( Fx \), respectively, an atom \( a \) defined by the rule ‘\( a \leftarrow b, \sim c \)’ gives rise to two nogoods: \( \{Ta, Fx_{\{b, \sim c\}}\} \) and \( \{Fa, Tx_{\{b, \sim c\}}\} \), where \( x_{\{b, \sim c\}} \) is an auxiliary variable for the body of the rule. Similarly, the body \( \{b, \sim c\} \) leads to nogoods \( \{Fx_{\{b, \sim c\}}, Tb, Fc\} \), \( \{Tx_{\{b, \sim c\}}, Fb\} \), and \( \{Tx_{\{b, \sim c\}}, Tc\} \). The last nogood precludes solutions assigning true to both variables \( x_{\{b, \sim c\}} \) and \( c \). See (Gebser et al. 2012) for full details.

Once a logic program is translated accordingly, we can take advantage of Conflict-Driven Constraint Learning (CDCL; (Marques-Silva and Sakallah 1999; Zhang et al. 2001)) for computing the solutions of the obtained set of nogoods. The basic algorithm is outlined in Fig. 1. The CDCL algorithm first extends a given (partial) assignment via deterministic (unit) propagation. Importantly, every derived literal is “forced” by some nogood (seen as a set of signed literals that must not jointly be assigned), which would be violated if the literal’s complement were assigned. Although propagation aims at forgoing nogood violations, assigning a literal forced by one nogood may lead to the violation of another nogood; this situation is called conflict. If the conflict can be resolved (the violated nogood contains backtrackable literals), it is analyzed to identify a conflict
loop
  propagate // compute deterministic consequences
  if no conflict then
    if all variables assigned then return variable assignment
    else decide // non-deterministically assign some literal
  else
    if top-level conflict then return unsatisfiable
    else
      analyze // analyze conflict and add a conflict constraint
      backjump // undo assignments until conflict constraint is unit
Fig. 1. Basic algorithm for conflict-driven Boolean constraint learning (CDCL)

constraint. The latter represents a “hidden” conflict reason that is recorded and guides backjumping to an earlier stage such that the complement of some formerly assigned literal is forced by the conflict constraint, thus triggering propagation. Only when propagation finishes without conflict, a (heuristically chosen) literal can be assigned at a new decision level, provided that the assignment at hand is partial, while a solution (total assignment not violating any nogood) has been found otherwise. The eventual termination of CDCL is guaranteed, by either returning a solution or encountering an unresolvable conflict (independent of unforced decision literals). In practice, CDCL employs further operations promoting the search process. One such operation consists in occasionally restarting the search process in order to escape from unfruitful search spaces while keeping gathered information. This could be added to Fig. 1 by replacing “decide” by “decide or restart”. Another crucial operation is nogood deletion given that an exponential number of nogoods is learnable. Conceptually, this is commonly performed after propagate in Fig. 1.

3 Data logging and visualization

As sketched in the introductory section, our overall approach is two-fold, consisting of an online data logging phase along with an offline (visual) analysis phase.

Online data logging. The data logger protocols events relevant to CDCL-based solving during an actual run of an ASP solver.

To begin with, it records all deterministic consequences derived in propagate and non-deterministic assignments done by decide along with the respective decision levels. These events can already be used to extract various interesting figures, like how often did a variable change its truth value, how often is a variable implied or chosen, how many propagations follow a particular choice, at which decision level was a variable implied or chosen, etc.

An operation crucial to CDCL is conflict analysis, accomplished by analyze. Central to this is a resolution derivation, resolving conflict constraints with constraints used in unit propagation. All such derivations are recorded during data logging. This also provides the resulting conflict constraint, which is learned by CDCL. Moreover this allows us to track how often variables (jointly) occur in conflict resolutions and the resulting conflict constraints. In fact, conflict information is central to CDCL because it is used for various heuristics, as for instance in decide and constraint deletion. Notably, the generality of our approach allows for monitoring and comparing different decision heuristics in a uniform setting. For example, heuristics like berkmin (Goldberg
and Novikov 2002) or vsids (Moskewicz et al. 2001) rely on different ways of scoring variables according to their conflict involvement.

Similarly, the data logger records all backjump and restart operations along with the respective decision levels. This involves the skipped decision levels as well as data on backtracked assignments. Similar to the above, this can moreover be combined with data on the subsequent propagate operation for determining the resulting deterministic consequences.

Finally, the data logger also keeps track of constraint deletion and incorporates static data, like program constraints, resulting stable models, and symbol tables, one mapping original atoms to grounder identifiers and another mapping original and auxiliary atoms to solver identifiers. Although the logger’s implementation is necessarily solver-specific, our design was driven by the desire to extract only information pertinent to the CDCL-based solving process and to exclude any implementation-specific data. As a result, our data logger produces a database comprising an event series reflecting the ASP solving process along with some static data. The obtained information can then be used in various ways by different back-ends.

Offline visual analysis. Our primary back-end aims at visualizing the gathered information to provide insights into the ASP solving process. To this end, we (currently) focus on structural and temporal perspectives.

Structural aspects. For capturing structural aspects, we concentrate on interaction graphs\(^1\) being undirected graphs providing a uniform abstraction of often richer yet dedicated structures. While the set of vertices is fixed to (a subset of) the solver’s propositional variables, the set of edges varies in view of the type of interaction to be displayed. In its original definition, the interaction graph connects two variables whenever they are contained in the same program clause. Extending this concept, we provide graphs displaying interactions indicating containment in the same program constraint (cf. Fig. 2), learned nogood, resolution derivation, or conflict nogood. Unlike these, the choice tree graph contains only variables that have been non-deterministically assigned (in decide); it links two variables whenever one was decided after the other (without intermediate backjump or restart).

Given that interaction graphs have no predefined layout, we follow (Sinz and Dieringer 2005) in using a force-directed graph drawing algorithm (Hachul and Jünger 2004) for rendering. These algorithms assign forces among nodes for obtaining edges of balanced length (and as few crossings as possible). We refine the graphical layout by weighting the force between nodes through interaction-dependent factors. For instance, when laying out the program interaction graph, we amplify the force among two variables according to their number of joint occurrences in program constraints. Hence, roughly speaking, variables connected by a short edge have more such joint occurrences than variable connected by longer edges. These weights are calculated via a scoring similar to the MOMs heuristic (Pretolani 1996). Analogous weights are used for displaying the other aforementioned graph structures. This option does not provoke a complete re-structuring but helps exposing certain structures. For illustration, consider the program interaction graph in Fig. 2 where our graph layout leads to a state-wise clustering of variables.

Apart from furnishing different structural views, the purpose of interaction graphs is to offer projection surfaces for complementary information. A simple yet instructive such combination is graph overlay. The idea is to display the edges of one graph with the node layout of another. For

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1 These graphs were used in (Sinz and Dieringer 2005) for visualizing SAT; cf. (Rish and Dechter 2000; Sinz 2007).
instance, this allows us to study the interaction in learned nogoods in the context of the original problem structure. Another simple yet very effective combination is obtained by graph coloring. In fact, the data logger gathers several figures for each node during the solving process. Among these aggregated values on variables, we consider the number of decisions, number of conflict analyses, or the number of flipped values. These values can be aggregated over the whole solving process (by default) or any user-defined period of events (see temporal aspects below). The result is then projected through node colors on the interaction graph at hand. For this purpose, we use the color sequence from red to green. For instance in Fig. 2, we color variable nodes according to how often their values have been flipped. Accordingly, the variable having been flipped most often is colored in deep red, while 11 of 467 variables have been assigned only once and are thus in deep green. Notably, graph overlay and coloring can be freely combined. As mentioned, the coloring may reflect data collected during the entire or just a selected fragment of the solving process.

The inspection of node-specific information is supported by two complementary means. First, we integrate the aggregated values into the symbol table. Second, we offer a simple query language for filtering the displayed set of variable nodes. Finally, both capacities are dynamically linked to graph coloring and seamlessly adapt to changes triggered by the user in either of the three contexts.

A symbol table consists of four types of entries: a variable’s solver identifier, its type, value, and symbolic representation. Each variable has a unique integer as solver identifier and may have one of three types: atom, body, or atom/body. The symbolic representation is type-specific: While a variable of type atom is associated with a unique ground atom, no representation is available for type body. The type atom/body represents multiple equivalent variables (e.g., obtained through pre-processing) and gives all ground atoms associated with the solver identifier. The variable’s value is mode-dependent and corresponds to the aggregated value used for coloring. Also, the (visible entries of the) symbol table can be sorted according to any attribute. For instance in Fig. 2, the node with the deepest red corresponds to the following entry.

<table>
<thead>
<tr>
<th>id</th>
<th>type</th>
<th>value</th>
<th>symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>26</td>
<td>atom/body</td>
<td>23</td>
<td>move(4,c,5)</td>
</tr>
</tbody>
</table>

Given that the coloring in Fig. 2 reflects the number of times that the value of the variable was flipped, the entry tells us that the atom move(4,c,5) was flipped 23 times.

The elements shown in the symbol table as well as the colored graph can be controlled via a simple query language. The language uses keywords id:, type:, and val: to refer to an entry’s attributes; simple expressions (including wild card *) are used for matching symbolic representations. The keywords are followed by values of the respective type, except that val: additionally allows for simple range specifications of form > i or < i for some integer i. A conjunction is simply a blank; a disjunction is expressed by ‘;’. For instance in the context of Fig. 2, the query ‘type:atom move(*) val:>4 val:<12’ selects all atoms formed from predicate move that have been flipped more than four and less than twelve times.

The interplay between the colored graph, the symbol table, and the query engine is designed to be highly dynamic. For instance, hovering over nodes in the graph centers the symbol table and highlights the corresponding entry. Selecting a cell in the symbol table produces the corresponding query and restricts coloring to the selected variables. And finally, posing a query selects the corresponding entries in the symbol table and restricts coloring accordingly. See Section 4 for more detailed information.
Temporal aspects. We capture temporal aspects by means of two-dimensional plots. While our interaction graphs provide views on the internal problem structure using aggregated node information, we use plots to provide insights into the dynamics of the solving process by exposing the development of its key figures. Instead of time, however, we use the sequence of conflicts, choices, or other events depending on the respective displayed aspect.\(^2\)

The respective plots are enriched with the absolute and central moving average (over neighboring data points) as well as the median value. As an example, consider the left plot in Fig. 3, showing the length of each nogood in recording order. Accordingly, the \(x\)-axis is organized along conflicts (rather than choices). (The \(y\)-axis can be arranged in linear or logarithmic scale.) Alternatively, a frequency distribution can be provided, as done in the right plot in Fig. 3. The design of the interface was done to support the user in exploring the solving process. To this end, one may interactively select fragments of the plot and navigate through these fragments. Importantly, the selected solving spans may be used to build graphs reflecting the structural view and/or aggregated variable values collected in these segments.

4 The clavis and insight systems

In what follows, we describe the usage along with some implementation details of our data logger clavis and our visualization tool insight. We illustrate the usage of clavis and insight through a small use-case. For this purpose, we consider the Towers of Hanoi problem from (Gebser et al. 2012). Both systems and the problem encoding are available at (clavis).

clavis is a full-fledged ASP solver corresponding to clasp (2.1; (Gebser et al. 2012)) yet enhanced by data logging capacities. In fact, clavis is distributed as a patch to clasp, which facilitates its maintenance over progressing clasp versions. Apart from the obligatory name of the resulting database file, clavis allows for supplying a configuration file delineating the logged events along with the full set of (single-threaded) options of clasp. clavis also tolerates partial runs obtained either by clasp’s option ‘\(--\text{time-limit}\)’ or user interrupts through SIGINT. For example, we may produce the event database toh.h5 by the command (where ‘\(--\text{heuristics=vslids}\)’ is an example clasp option):

gringo tohI.lp tohE.lp | clavis --heuristics=vslids toh

The resulting data is stored in an HDF5\(^3\) database; it includes separate tables for each event type and a global index along with static data such as symbol tables. This approach allows for fast iteration of single event types as well as flexibility in logging. For instance, excluding some event types like propagations can significantly reduce the log size. Also, the logfile can be extended by additional events or meta data without breaking existing back-ends.

Different back-ends can be used for analyzing the logged information. Although it is possible to read the logfile directly via a library like pytables, we furnish an interface for sequential access and analysis through clavis’ library libclavis. The benefits of this approach compared to direct access are much shorter read times due to caching and a simplified interface abstracting from the complexity of HDF5. All generated data is stored using widely-used libraries such as networkx for graphs and numpy for sequential data. This allows for simple generation of derived data like centrality measures for graphs or frequency distribution for sequential data. The full documentation of the log format and examples using libclavis can be found at (clavis).

\(^2\) For example, \(2\) on the \(x\)-axis refers to the second event.

\(^3\) http://www.hdfgroup.org/HDF5
*insight* is launched either directly or by passing the event database, viz. *insight toh.h5*. After loading a logfile, *insight* displays the list of open views (and the *problem view*).

Let us explain some distinguished features of *insight* by looking at some screenshots in Fig. 2 to 4. On the left of all three, we see the *view list* giving all currently active (white on blue) and inactive (black on white) views; they can be (de)activated by mouse selection. The *problem view* in the middle of Fig. 2 is the default view after loading the logfile. At its top, it summarizes the key figures of the solving process at hand. Below, the actual visualization is configured and engaged, distinguishing the aforementioned structural (‘Graph’) and temporal views (‘Plot’).

The displayed setting allows for generating the program interaction graph. The resulting view is given on the right of Fig. 2. The graph nicely reflects the temporal structure of the Towers of Hanoi problem by grouping variables in a state-wise fashion. That is, variables with the same time stamp form clusters along the graph. The structure can be explored with zooming and panning functionalities (including reset button) and the visualization can be focused (while all other views are hidden). Note that the orientation of the graph is subject to random factors within the force-directed layout (e.g. the graph might be mirrored for slightly varying data). However, the layout algorithm is seeded to assure that the same input leads to the same layout. Different layout engines can be used; currently, *insight* offers the choice between the *FMMLayout* from *OGDF* and *sfdp* from *Graphviz*. The position of a variable can be inferred from the highlighting of the symbol table while hovering with the mouse over the node in the graph, or simply by searching for symbols via pattern matching (e.g. for *move(1,1)*). The variable coloring in Fig. 2 reflects the number of flipped truth assignments. Inspecting the graph in conjunction with the symbol table reveals that the “hot-spot” of the problem concerns action and fluent variables with time stamps 3-6, changing their truth values more than twenty times (as shown in the symbol table). While these variables are in deeper red, the ones in the upper left part of the graph are colored in deeper green indicating that their truth value was rarely changed. This tells us that the goal conditions\(^4\) are strong enough to fix the truth values of variables close to the final state. In fact, this can be made precise by posing a simple query like ‘*val:<5*’ (similar to the left view in Fig. 4).

\(^4\) That is, the goal state defined by *goal_on/2*. 
To complement this, let us look at the development of the conflict level during the solving process in the left view in Fig. 3. To support this, we show on the right the frequency distribution of the number of decisions per conflict; this provides an idea on the progress made during the 155 conflicts on the x-axis on the left. For instance, 52 times no decision was made between two conflicts; here, the learned nogoods caused an(other) immediate conflict. 36 conflicts were obtained after a single decision. Now, following the (green) central moving average in the left view, we observe two peaks dividing the solving process into three parts. Our hypothesis is that a part of the problem has been solved during the first solving phase. To explore this further, we take advantage of insight’s zooming and panning capacities. That is, via mouse control, we select the last two segments of the solving process and generate (i) the program interaction graph colored according to the numbers of flipped assignments during this span along with (ii) the learned nogoods interaction yet projected on the program interaction graph colored in the same way (for comparability). The result is shown in Fig. 4. In fact, the coloring on the left is further constrained by restricting the view to variables whose truth values remain unchanged during the last two parts of the solving process. This selection is accomplished via the simple query ‘val:0’. The resulting cloud of green nodes supports our conjecture that the truth value of the obtained variables has been fixed in the first part of the solving process. More evidence for this is provided by conflict learning because nothing has been learned about this program part during the considered span of events. This can be visualized by the projection of the learned nogood interactions onto the program interaction graph on the right of Fig. 4: The green nodes in the left view do not appear in the right one. Hence, they do not appear in any nogoods learned in the last two phases of the solving process.

Important for the analysis of the ASP solving process is the consideration of larger problem sizes. With only 1200 variables and 1800 constraints, the presented Towers of Hanoi example is
a small problem compared to many real world examples. We employ a variety of techniques to handle larger problems by raising both the efficiency and flexibility of our tools. clavis stores the recorded data in a database designed to handle high volumes of data efficiently and in a format that is configurable to select the logged events. libclavis and insight are built upon libraries for efficient processing and presentation of information. This allows us to handle larger problems in the range of around 30,000 variables and 100,000 constraints for which the generation times of the different visualizations lie between a few seconds to two minutes on an Intel Core i7 processor. However, the specific runtimes are highly dependent on each specific problem.

5 Related work

There are several works using similar techniques in the area of SAT. Most influential to our work are dpvis and 3dvis (Sinz and Dieringer 2005; Sinz 2007) as they also use interaction graphs to visualize the structure of SAT problems. Additionally, dpvis features online visualization through integration with a SAT solver for updating both the graph structure (e.g. for learned clauses) and colors (for assigned values) to reflect the current solving state. As mentioned above, our approach adapts the concept of representing program structure via interaction graphs and extends it to various types of interactions. Similarly, we also allow for the combination of program interaction graphs and learned nogoods but as part of a more general scheme involving multiple structural aspects of the solving process. Our offline visualization approach loses the interaction with the solver shown in dpvis but allows for much more freedom in combining and aggregating data from different parts of the solving process enabling the analysis of larger problems for which the approach of dpvis is impracticable. Furthermore, by including the symbol table of the ASP solver, we obtain a much deeper understanding of the problem’s structure.

6 Conclusion

The presented visualization toolchain consists of a two-step approach for exploring ASP solving processes. The data logger clavis provides a configurable tool for collecting data during ASP solving and storing it in an easily accessible database format, viz HDF5. Apart from providing various structural and temporal views on the ASP solving process, the visualization tool insight
is designed to foster the exploration of the solving process by providing the user with interactive means for changing the perspective on selected structures.

This work will be continued by collecting data from the grounding process as well as creating new visualizations for all gathered data. The goal of this project is to provide a comprehensive look at the processes inside ASP solvers and the structure of the solved problems. The direct effect of these efforts will be more efficient ASP solvers and improved encodings. However, my hope is that it will also lead to a better understanding of the structure inherent to the problems themselves regardless of their ASP encodings.

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References


