Towards embedded Answer Set Solving

Torsten Schaub

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Torsten Schaub (KRR@UP)

Outline

1 Introduction

- 2 Foundations
- 3 Modeling
- 4 Modeling and Controlling
- 5 Case-study: Ricochet Robots
- 6 Case-sketch: Preferences and optimization
- 7 Potassco
- 8 Summary



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Answer Set Programming (ASP)

ASP is an approach to declarative problem solving

describe the problem, not how to solve it

ASP allows for solving hard search and optimization problems

- Systems Biology
- Product Configuration
- Linux Package Configuration
- Robotics
- Music Composition
-

All search-problems in NP (and NP^{NP}) are expressible



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■ All search-problems in *NP* (and *NP^{NP}*) are expressible





Expressive modeling language Powerful grounding and solving tools



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Propositional Normal Logic Programs

 \blacksquare A logic program Π is a set of rules of the form

$$\underbrace{a}_{\text{head}} \leftarrow \underbrace{b_1, \ldots, b_m, \sim c_1, \ldots, \sim c_n}_{\text{body}}$$

■ a and all b_i, c_j are atoms (propositional variables) ■ \leftarrow , ,, \sim denote if, and, and default negation

- Semantics given by stable models, informally, sets X of atoms such that
 X is a (classical) model of Π and
 each atom in X is justified by some rule in Π



Logic Programs

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a and all b_i, c_j are atoms (propositional variables)
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Logic Programs as Propositional Formulas $\Pi = \{ a \leftarrow \sim b \quad b \leftarrow \sim a \quad x \leftarrow a, \sim c \quad x \leftarrow y \quad y \leftarrow x, b \}$ $CF(\Pi) = \{ a \leftarrow \neg b \quad b \leftarrow \neg a \quad x \leftarrow (a \land \neg c) \lor y \quad y \leftarrow x \land b \}$ $\cup \{ c \leftrightarrow \bot \}$ $LF(\Pi) = \{ (x \lor y) \rightarrow a \land \neg c \}$

Classical models of $CF(\Pi)$: {b}, {b,c}, {b,x,y}, {b,c,x,y}, {a,c}, {a,b,c}, {a,x}, {a,c,x}, {a,x,y}, {a,c,x,y}, {a,b,x,y}, {a,b,c,x,y}

Unsupported atoms Unfounded atoms



 $\Pi = \left\{ a \leftarrow \sim b \quad b \leftarrow \sim a \quad x \leftarrow a, \sim c \quad x \leftarrow y \quad y \leftarrow x, b \right\}$ $RF(\Pi) = \left\{ a \leftarrow \neg b \quad b \leftarrow \neg a \quad x \leftarrow (a \land \neg c) \lor y \quad y \leftarrow x \land b \right\}$ $\cup \left\{ c \leftrightarrow \bot \right\}$ $LF(\Pi) = \left\{ (x \lor y) \rightarrow a \land \neg c \right\}$

Classical models of $RF(\Pi)$: (only true atoms shown) {b}, {b,c}, {b,x,y}, {b,c,x,y}, {a,c}, {a,b,c}, {a,x}, {a,c,x}, {a,x,y}, {a,c,x,y}, {a,b,c,x,y}

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Classical models of $CF(\Pi)$: {b}, {b,c}, {b,x,y}, {b,c,x,y}, {a,c}, {a,b,c}, {a,x}, {a,c,x}, {a,x,y}, {a,c,x,y}, {a,b,x,y}, {a,b,c,x,y}

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Classical models of $CF(\Pi) \cup LF(\Pi)$: {b}, {b,c}, {b,x,y}, {b,c,x,y}, {a,c}, {a,b,c}, {a,x}, {a,c,x}, {a,x,y}, {a,c,x,y}, {a,b,x,y}, {a,b,c,x,y}

- Unsupported atoms
- Unfounded atoms



 $\Pi = \left\{ a \leftarrow \sim b \quad b \leftarrow \sim a \quad x \leftarrow a, \sim c \quad x \leftarrow y \quad y \leftarrow x, b \right\}$

 $CF(\Pi) = \left\{ a \leftrightarrow \left(\bigvee_{(a \leftarrow B) \in \Pi} BF(B) \right) \mid a \in atom(\Pi) \right\}$ $BF(B) = \bigwedge_{b \in B \cap atom(\Pi)} b \land \bigwedge_{\sim c \in B} \neg c$ $LF(\Pi) = \left\{ \left(\bigvee_{a \in L} a \right) \rightarrow \left(\bigvee_{a \in L, (a \leftarrow B) \in \Pi, B \cap L = \emptyset} BF(B) \right) \mid L \in loop(\Pi) \right\}$ Classical models of $CF(\Pi) \cup LF(\Pi)$:

Theorem (Lin and Zhao)

Let Π be a normal logic program and $X \subseteq atom(\Pi)$. Then, X is a stable model of Π iff $X \models CF(\Pi) \cup LF(\Pi)$.

Size of CF(Π) is linear in the size of Π
 Size of LF(Π) may be exponential in the size of Π



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Some language constructs

Variables \blacksquare p(X) :- q(X) over constants {a, b, c} stands for p(a) := q(a), p(b) := q(b), p(c) := q(c)Conditional Literals \blacksquare p :- q(X) : r(X) given r(a), r(b), r(c) stands for p := q(a), q(b), q(c)Disjunction \square p(X) ; q(X) :- r(X) Integrity Constraints \blacksquare :- q(X), p(X) Choice **2** { p(X,Y) : q(X) } 7 :- r(Y)Aggregates ■ s(Y) :- r(Y), 2 #sum { X : p(X,Y), q(Y) } 7

Basic methodology

Methodology

Generate and Test (or: Guess and Check)

Generator Generate potential stable model candidates (typically through non-deterministic constructs) Tester Eliminate invalid candidates (typically through integrity constraints)

Peanutshell

Logic program = Data + Generator + Tester (+ Optimizer)

Potassco

Basic methodology

Methodology

Generate and Test (or: Guess and Check)

Generator Generate potential stable model candidates (typically through non-deterministic constructs) Tester Eliminate invalid candidates (typically through integrity constraints)

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Logic program = Data + Generator + Tester (+ Optimizer)

Potassco

Satisfiability testing $(a \leftrightarrow b) \land c$



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Satisfiability testing $(a \leftrightarrow b) \land c$

{ a ; b ; c }.

- :- not a, b.
- :- a, not b.
- :- not c.



Maximum satisfiability testing $"(a \nleftrightarrow b)" + (a \leftrightarrow b) \land c$





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n-queens Basic encoding

{ queen(1..n,1..n) }.

```
:- { queen(I,J) } != n.
:- queen(I,J), queen(I,JJ), J != JJ.
:- queen(I,J), queen(II,J), I != II.
:- queen(I,J), queen(II,JJ), (I,J) != (II,JJ), I-J = II-JJ.
:- queen(I,J), queen(II,JJ), (I,J) != (II,JJ), I+J = II+JJ.
```



n-queens Advanced encoding

{ queen(I,1..n) } = 1 :- I = 1..n. { queen(1..n,J) } = 1 :- J = 1..n.

:- { queen(D-J,J) } >= 2, D = 2..2*n. :- { queen(D+J,J) } >= 2, D = 1-n..n-1.



n-queens (Experimental) constraint encoding

```
1 $<= $queen(1..n) $<= n.
#disjoint { X : $queen(X) $+ 0 : X=1..n }.
#disjoint { X : $queen(X) $+ X : X=1..n }.
#disjoint { X : $queen(X) $- X : X=1..n }.</pre>
```



Traveling salesperson Basic encoding (no instance)

```
1 { cycle(X,Y) : edge(X,Y) } 1 :- node(X).
1 { cycle(X,Y) : edge(X,Y) } 1 :- node(Y).
```

```
reached(X) :- X = #min { Y : node(Y) }.
reached(Y) :- cycle(X,Y), reached(X).
```

:- node(Y), not reached(Y).

#minimize { C,X,Y : cycle(X,Y), cost(X,Y,C) }.


Company Controls

```
controls(X,Y) :-
    #sum+ { S: owns(X,Y,S);
        S,Z: controls(X,Z), owns(Z,Y,S) } > 50,
        company(X), company(Y), X != Y.
```

<pre>company(c_1).</pre>	owns(c_1,c_2,60).
	owns(c_1,c_3,20).
<pre>company(c_2).</pre>	owns(c_2,c_3,35).
<pre>company(c_3).</pre>	owns(c_3,c_4,51).
company(c, 4)	



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Claim ASP is an under-the-hood technology

That is, in practice, it mainly serves as a solving engine within an encompassing software environment

Single-shot solving: ground | solve
 Multi-shot solving: ground | solve

➡ continuously changing logic programs

Agents, Assisted Living, Robotics, Planning, Query-answering, etc *clingo* 4 — providing operative solving processes dealing with continously changing logic programs



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■ Multi-shot solving: (*input* | *ground** | *solve**)*

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■ Single-shot solving: *ground* | *solve*

- Multi-shot solving: (input | ground* | solve* | theory)*
 - continuously changing logic programs

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That is, in practice, it mainly serves as a solving engine within an encompassing software environment

■ Single-shot solving: *ground* | *solve*

- Multi-shot solving: (input | ground* | solve* | theory | ...)*
 - ➡ continuously changing logic programs

Application areas

Agents, Assisted Living, Robotics, Planning, Query-answering, etc



Claim ASP is an under-the-hood technology

That is, in practice, it mainly serves as a solving engine within an encompassing software environment

Single-shot solving: ground | solve
 Multiplication (include solution)

- Multi-shot solving: (input | ground* | solve* | theory | ...)*
 - continuously changing logic programs

Application areas

Agents, Assisted Living, Robotics, Planning, Query-answering, etc



Claim ASP is an under-the-hood technology

That is, in practice, it mainly serves as a solving engine within an encompassing software environment

Single-shot solving: *ground* | *solve*

- Multi-shot solving: (*input* | *ground** | *solve** | *theory* | ...)*
 - continuously changing logic programs
- Application areas

Agents, Assisted Living, Robotics, Planning, Query-answering, etc



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That is, in practice, it mainly serves as a solving engine within an encompassing software environment

Single-shot solving: *ground* | *solve*

- Multi-shot solving: (*input* | *ground** | *solve** | *theory* | ...)*
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- Multi-shot solving: (*input* | *ground** | *solve** | *theory* | ...)*
 - continuously changing logic programs
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ASF

Contro

Integration

in ASP: embedded scripting language (#script in Lua/Python: library import (import gringo



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ASP

Contro

```
Lua (www.lua.org)
    prg:solve(), prg:ground(parts), ...
Python (www.python.org)
    prg.solve(), prg.ground(parts), ...
```

Integration

in ASP: embedded scripting language (#script in Lua/Python: library import (import gringo



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ASP #program <name> [(<parameters>)] Example #program play(t). #external <atom> [: <body>] Example #external mark(X,Y,P,t) : field(X,Y), player(P).

Contro

Integration

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ASP #program <name> [(<parameters>)] Example #program play(t). #external <atom> [: <body>] Example #external mark(X,Y,P,t) : field(X,Y), player(P). Control Lua (www.lua.org) Example prg:solve(), prg:ground(parts), ...

- Python (www.python.org)
 - Example prg.solve(), prg.ground(parts), ...

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in ASP: embedded scripting language (#script) in Lua/Python: library import (import gringo)



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Example prg:solve(), prg:ground(parts), ...

Python (www.python.org)

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Lua (www.lua.org)

Example prg:solve(), prg:ground(parts), ...

Python (www.python.org)

Example prg.solve(), prg.ground(parts), ...

Integration

in ASP: embedded scripting language (#script)

■ in Lua/Python: library import (import gringo)



Vanilla Clingo

■ Emulating *Clingo* in *Clingo* 4

```
#script (python)
def main(prg):
    parts = []
    parts.append(("base", []))
    prg.ground(parts)
    prg.solve()
#end.
```



Vanilla Clingo

Emulating Clingo in Clingo 4

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Towers of Hanoi Instance

■ Emulating *iClingo* (an incremental ASP solver) in *Clingo* 4

- Incremental grounding
- Incremental solving



Towers of Hanoi Instance



peg(a;b;c). init_on(1,a). init_on((2;7),b). init_on((3;4;5;6),c). disk(1..7).

goal_on((3;4),a).
goal_on((1;2;5;6;7),c).



Towers of Hanoi Encoding (base)

#program base.

```
on(D,P,0) :- init_on(D,P).
```



Towers of Hanoi Encoding (cumulative)

```
#program cumulative(t).
```

```
1 { move(D,P,t) : disk(D), peg(P) } 1.
```

```
moved(D,t) :- move(D,_,t).
blocked(D,P,t) :- on(D+1,P,t-1), disk(D).
blocked(D,P,t) :- blocked(D+1,P,t), disk(D).
:- move(D,P,t), blocked(D-1,P,t).
:- moved(D,t), on(D,P,t-1), blocked(D,P,t).
```

```
on(D,P,t) :- on(D,P,t-1), not moved(D,t).
on(D,P,t) :- move(D,P,t).
:- not 1 { on(D,P,t) : peg(P) } 1, disk(D).
```



Towers of Hanoi Encoding (volatile)

```
#program volatile(t).
#external query(t).
```

```
:- goal_on(D,P), not on(D,P,t), query(t).
```

Exercising control

An #external atom can be controlled from Python (or Lua) via

- assign_external(self,atom,value)
 where value is either True, False, or None
- release_external(self,atom) sets atom permanently to False



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Incremental Solving (embedded)

```
#script (python)
```

```
from gringo import SolveResult, Fun
```

```
def main(prg):
    ret, parts, step = SolveResult.UNSAT, [], 1
    parts.append(("base", []))
    while ret == SolveResult.UNSAT:
        parts.append(("cumulative", [step]))
        parts.append(("volatile", [step]))
        parts.append(("volatile", [step]))
        prg.ground(parts)
        prg.release_external(Fun("query", [step-1]))
        prg.assign_external(Fun("query", [step]), True)
        ret, parts, step = prg.solve(), [], step+1
```

#end.

Potassco

Incremental Solving (library)

```
from sys import stdout
from gringo import SolveResult, Fun, Control
prg = Control()
prg.load("toh.lp")
ret, parts, step = SolveResult.UNSAT, [], 1
parts.append(("base", []))
while ret == SolveResult.UNSAT:
    parts.append(("cumulative", [step]))
    parts.append(("volatile", [step]))
    prg.ground(parts)
    prg.release_external(Fun("query", [step-1]))
   prg.assign_external(Fun("query", [step]), True)
    f = lambda m: stdout.write(str(m))
    ret, parts, step = prg.solve(on_model=f), [], step+1
```

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Alex Rudolph's Ricochet Robots

Solving goal (13) from cornered robots



Four robots
 roaming
 horizontally
 vertically
 up to blocking objects,
 ricocheting (optionally)

 Goal Robot on target (sharing same color)



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Towards embedded Answer Set Solving





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board.lp

dim(1..16).

barrier(2, 1, 1, 0).	barrier(13,11, 1, 0).	barrier(9, 7, 0, 1).
barrier(10, 1, 1, 0).	barrier(11,12, 1, 0).	barrier(11, 7, 0, 1).
barrier(4, 2, 1, 0).	barrier(14,13, 1, 0).	barrier(14, 7, 0, 1).
barrier(14, 2, 1, 0).	barrier(6,14, 1, 0).	barrier(16, 9, 0, 1).
barrier(2, 3, 1, 0).	barrier(3,15, 1, 0).	barrier(2,10, 0, 1).
barrier(11, 3, 1, 0).	barrier(10,15, 1, 0).	barrier(5,10, 0, 1).
barrier(7, 4, 1, 0).	barrier(4,16, 1, 0).	barrier(8,10, 0,-1).
barrier(3, 7, 1, 0).	barrier(12,16, 1, 0).	barrier(9,10, 0,-1).
barrier(14, 7, 1, 0).	barrier(5, 1, 0, 1).	barrier(9,10, 0, 1).
barrier(7, 8, 1, 0).	barrier(15, 1, 0, 1).	barrier(14,10, 0, 1).
barrier(10, 8,-1, 0).	barrier(2, 2, 0, 1).	barrier(1,12, 0, 1).
barrier(11, 8, 1, 0).	barrier(12, 3, 0, 1).	barrier(11,12, 0, 1).
barrier(7, 9, 1, 0).	barrier(7, 4, 0, 1).	barrier(7,13, 0, 1).
barrier(10, 9,-1, 0).	barrier(16, 4, 0, 1).	barrier(15,13, 0, 1).
barrier(4,10, 1, 0).	barrier(1, 6, 0, 1).	barrier(10,14, 0, 1).
barrier(2,11, 1, 0).	barrier(4, 7, 0, 1).	barrier(3,15, 0, 1).
barrier(8,11, 1, 0).	barrier(8, 7, 0, 1).	



targets.lp

#external goal(1..16).

```
target(red, 5, 2) := goal(1).
target(red, 15, 2) :- goal(2).
target(green, 2, 3) := goal(3).
target(blue, 12, 3) :- goal(4).
target(yellow, 7, 4) := goal(5).
target(blue, 4, 7) :- goal(6).
target(green, 14, 7) := goal(7).
target(vellow.11, 8) :- goal(8).
target(yellow, 5,10) :- goal(9).
target(green, 2,11) :- goal(10).
target(red, 14,11) :- goal(11).
target(green, 11,12) :- goal(12).
target(vellow, 15, 13) :- goal(13).
target(blue, 7,14) :- goal(14).
target(red, 3.15) :- goal(15).
target(blue, 10,15) :- goal(16).
```

robot(red;green;blue;yellow).
#external pos((red;green;blue;yellow),1..16,1..16).



ricochet.lp

```
time(1..horizon).
dir(-1,0;1,0;0,-1;0,1).
stop( DX, DY,X, Y ) :- barrier(X,Y,DX,DY).
stop(-DX, -DY, X+DX, Y+DY) := stop(DX, DY, X, Y).
pos(R,X,Y,0) := pos(R,X,Y).
1 { move(R,DX,DY,T) : robot(R), dir(DX,DY) } 1 :- time(T).
move(R,T) := move(R, ...,T).
halt(DX, DY, X-DX, Y-DY, T) := pos(, X, Y, T), dir(DX, DY), dim(X-DX), dim(Y-DY),
                            not stop(-DX,-DY,X,Y), T < horizon.
goto(R, DX, DY, X, Y, T) := pos(R, X, Y, T), dir(DX, DY), T < horizon.
goto(R,DX,DY,X+DX,Y+DY,T) :- goto(R,DX,DY,X,Y,T), dim(X+DX), dim(Y+DY),
                          not stop(DX,DY,X,Y), not halt(DX,DY,X,Y,T).
pos(R,X,Y,T) :- move(R,DX,DY,T), goto(R,DX,DY,X,Y,T-1),
                not goto(R,DX,DY,X+DX,Y+DY,T-1).
pos(R,X,Y,T) :- pos(R,X,Y,T-1), time(T), not move(R,T).
:- target(R.X.Y), not pos(R.X.Y.horizon).
#show move/4.
```

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```
$ clingo board.lp targets.lp ricochet.lp -c horizon=9 \
        <(echo "pos(red,1,1). pos(green,16,1). pos(blue,1,16). pos(vellow,16,16). goal(13).")
clingo version 4.5.0
Reading from board.lp ...
Solving...
Answer: 1
move(red,0,1,1) move(red,1,0,2) move(red,0,1,3)
                                                        move(red, -1, 0, 4) move(red, 0, 1, 5) \setminus
move(yellow,0,-1,6) move(red,1,0,7) move(yellow,0,1,8) move(yellow,-1,0,9)
SATISFIABLE
Models
             : 1+
Calls
             : 1
Time
             : 1.895s (Solving: 1.45s 1st Model: 1.45s Unsat: 0.00s)
             : 1.880s
CPU Time
```

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```
$ clingo board.lp targets.lp ricochet.lp -c horizon=9 \
        <(echo "pos(red,1,1). pos(green,16,1). pos(blue,1,16). pos(vellow,16,16). goal(13).")
clingo version 4.5.0
Reading from board.lp ...
Solving...
Answer: 1
move(red,0,1,1) move(red,1,0,2) move(red,0,1,3)
                                                       move(red, -1, 0, 4) move(red, 0, 1, 5) \setminus
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             : 1.880s
CPU Time
$ clingo board.lp targets.lp ricochet.lp -c horizon=8 \
        <(echo "pos(red,1,1). pos(green,16,1). pos(blue,1,16). pos(vellow,16,16). goal(13).")
```

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```
$ clingo board.lp targets.lp ricochet.lp -c horizon=9 \
        <(echo "pos(red,1,1). pos(green,16,1). pos(blue,1,16). pos(vellow,16,16). goal(13).")
clingo version 4.5.0
Reading from board.lp ...
Solving...
Answer: 1
move(red, 0, 1, 1) move(red, 1, 0, 2) move(red, 0, 1, 3) move(red, -1, 0, 4) move(red, 0, 1, 5)
move(yellow,0,-1,6) move(red,1,0,7) move(yellow,0,1,8) move(yellow,-1,0,9)
SATISFIABLE
Models
           : 1+
Calls
           : 1
Time
            : 1.895s (Solving: 1.45s 1st Model: 1.45s Unsat: 0.00s)
           : 1.880s
CPU Time
$ clingo board.lp targets.lp ricochet.lp -c horizon=8 \
        <(echo "pos(red,1,1). pos(green,16,1). pos(blue,1,16). pos(vellow,16,16). goal(13).")
clingo version 4.5.0
Reading from board.lp ...
Solving...
UNSATISFIABLE
Models
             : 0
Calls
Time
             : 2.817s (Solving: 2.41s 1st Model: 0.00s Unsat: 2.41s)
                                                                                                    otassco
CPU Time
             : 2.800s
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```

optimization.lp

goon(T) := target(R,X,Y), T = 0..horizon, not pos(R,X,Y,T).

:- move(R,DX,DY,T-1), time(T), not goon(T-1), not move(R,DX,DY,T).

#minimize{ 1,T : goon(T) }.



```
$ clingo board.lp targets.lp ricochet.lp optimization.lp -c horizon=20 --quiet=1,0 \
       <(echo "pos(red,1,1). pos(green,16,1). pos(blue,1,16). pos(yellow,16,16).
                                                                                  goal(13).")
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```

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```
$ clingo board.lp targets.lp ricochet.lp optimization.lp -c horizon=20 --quiet=1,0 \
        <(echo "pos(red,1,1). pos(green,16,1). pos(blue,1,16). pos(yellow,16,16). goal(13).")
clingo version 4.5.0
Reading from board.lp ...
Solving...
Optimization: 20
Optimization: 19
Optimization: 18
Optimization: 17
Optimization: 16
Optimization: 15
Optimization: 14
Optimization: 13
Optimization: 12
Optimization: 11
Optimization: 10
Optimization: 9
Answer: 12
move(blue.0.-1.1)
                   move(blue.1.0.2)
                                        move(yellow,0,-1,3) move(blue,0,1,4)
                                                                                 move(yellow,-1,0,5) \
move(blue,1,0,6)
                    move(blue, 0, -1, 7)
                                        move(yellow,1,0,8) move(yellow,0,1,9)
                                                                                 move(yellow, 0, 1, 10) \setminus
move(vellow,0,1,11) move(vellow,0,1,12) move(vellow,0,1,13) move(vellow,0,1,14) move(vellow,0,1,15)
move(vellow.0.1.16) move(vellow.0.1.17) move(vellow.0.1.18) move(vellow.0.1.19) move(vellow.0.1.20)
OPTIMUM FOUND
Models
             : 12
 Optimum
             : ves
Optimization : 9
Calls
             : 1
Time
             : 16.145s (Solving: 15.01s 1st Model: 3.35s Unsat: 2.02s)
                                                                                                     otassco
CPU Time
             : 16.080s
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                                                                                                        37 / 60
```

Case-study: Ricochet Robots

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Playing in rounds

Round 1: goal(13)

Round 2: goal(4)

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Control loop

1 Create an operational *clingo* object

2 Load and ground the logic programs encoding Ricochet Robot (relative to some fixed horizon) within the control object

3 While there is a goal, do the following

- 1 Enforce the initial robot positions
- 2 Enforce the current goal
- 3 Solve the logic program contained in the control object



Ricochet Robot Player ricochet.py

```
from gringo import Control, Model, Fun
class Plaver:
    def init (self, horizon, positions, files);
        self.last_positions = positions
        self.last solution = None
        self.undo external = []
        self.horizon = horizon
        self.ctl = Control(['-c', 'horizon={0}'.format(self.horizon)])
        for x in files:
            self.ctl.load(x)
        self.ctl.ground([("base", [])])
    def solve(self, goal):
        for x in self.undo external:
            self.ctl.assign_external(x, False)
        self.undo external = []
        for x in self.last positions + [goal]:
            self.ctl.assign_external(x, True)
            self.undo_external.append(x)
        self.last solution = None
        self.ctl.solve(on_model=self.on_model)
        return self.last solution
    def on_model(self, model):
        self.last solution = model.atoms()
        self.last_positions = []
        for atom in model.atoms(Model.ATOMS):
            if (atom.name() == "pos" and len(atom.args()) == 4 and atom.args()[3] == self.horizon):
                self.last_positions.append(Fun("pos", atom.args()[:-1]))
horizon = 15
encodings = ["board.lp", "targets.lp", "ricochet.lp", "optimization.lp"]
positions = [Fun("pos", [Fun("red"),
                                       1, 1]), Fun("pos", [Fun("blue"),
                                                                               1. 16]).
            Fun("pos", [Fun("green"), 16, 1]), Fun("pos", [Fun("yellow"), 16, 16])]
sequence = [Fun("goal", [13]), Fun("goal", [4]), Fun("goal", [7])]
player = Player(horizon, positions, encodings)
for goal in sequence:
    print player.solve(goal)
```

- \blacksquare last positions holds the starting positions of the robots for each turn
- last_solution holds the last solution of a search call (Note that callbacks cannot return values directly)
- undolexternal holds a list containing the current goal and starting positions to be cleared upon the next step
- horizon holds the maximum number of moves to find a solution
- ctl holds the actual object providing an interface to the grounder and solver; it holds all state information necessary for multi-shot solving



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Ricochet Robot Player Setup and control loop

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from gringo import Control, Model, Fun
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        for x in files:
            self.ctl.load(x)
        self.ctl.ground([("base", [])])
    def solve(self, goal):
        for x in self.undo external:
            self.ctl.assign_external(x, False)
        self.undo external = []
        for x in self.last positions + [goal]:
            self.ctl.assign_external(x, True)
            self.undo_external.append(x)
        self.last solution = None
        self.ctl.solve(on_model=self.on_model)
        return self.last solution
    def on_model(self, model):
        self.last solution = model.atoms()
        self.last_positions = []
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encodings = ["board.lp", "targets.lp", "ricochet.lp", "optimization.lp"]
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                                                                              1. 16]).
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Initializing variables

2 Creating a player object (wrapping a *clingo* object)

3 Playing in rounds

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```
>> horizon = 15
>> encodings = ["board.lp", "targets.lp", "ricochet.lp", "optimization.lp"]
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1 Initializing variables

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```
>> print player.solve(goal)
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1 Initializing variables

- 2 Creating a player object (wrapping a *clingo* object)
- 3 Playing in rounds



```
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1 Initializing variables

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Ricochet Robot Player

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        for x in files:
            self.ctl.load(x)
        self.ctl.ground([("base", [])])
    def solve(self, goal):
        for x in self.undo_external:
            self.ctl.assign_external(x, False)
        self.undo external = []
        for x in self.last positions + [goal]:
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```
__init__
```

```
def __init__(self, horizon, positions, files):
    self.last_positions = positions
    self.last_solution = None
    self.undo_external = []
    self.horizon = horizon
    self.ctl = Control(['-c', 'horizon={0}'.format(self.horizon)])
    for x in files:
        self.ctl.load(x)
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```

- Initializing variables
- 2 Creating clingo object
- 3 Loading encoding and instance
- 4 Grounding encoding and instance


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>>

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- 2 Creating *clingo* object
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    self.ctl.ground([("base", [])])
```

- **1** Initializing variables
- 2 Creating *clingo* object
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Ricochet Robot Player

```
from gringo import Control, Model, Fun
class Plaver:
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    def solve(self, goal):
        for x in self.undo_external:
            self.ctl.assign_external(x, False)
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horizon = 15
encodings = ["board.lp", "targets.lp", "ricochet.lp", "optimization.lp"]
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                                       1, 1]), Fun("pos", [Fun("blue"),
                                                                              1. 16]).
            Fun("pos", [Fun("green"), 16, 1]), Fun("pos", [Fun("yellow"), 16, 16])]
sequence = [Fun("goal", [13]), Fun("goal", [4]), Fun("goal", [7])]
player = Player(horizon, positions, encodings)
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```

```
def solve(self, goal):
    for x in self.undo_external:
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    for x in self.last_positions + [goal]:
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    self.last_solution = None
    self.ctl.solve(on_model=self.on_model)
    return self.last_solution
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Unsetting previous external atoms (viz. previous goal and positions)
 Setting next external atoms (viz. next goal and positions)
 Computing next stable model by passing user-defined on model method

Potassco

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Potassco

Ricochet Robot Player on_model

```
from gringo import Control, Model, Fun
class Plaver:
    def init (self, horizon, positions, files);
        self.last_positions = positions
        self.last solution = None
        self.undo external = []
        self.horizon = horizon
        self.ctl = Control(['-c', 'horizon={0}'.format(self.horizon)])
        for x in files:
            self.ctl.load(x)
        self.ctl.ground([("base", [])])
    def solve(self, goal):
        for x in self.undo external:
            self.ctl.assign_external(x, False)
        self.undo external = []
        for x in self.last positions + [goal]:
            self.ctl.assign_external(x, True)
            self.undo_external.append(x)
        self.last solution = None
        self.ctl.solve(on_model=self.on_model)
        return self.last solution
    def on_model(self, model):
        self.last solution = model.atoms()
        self.last_positions = []
        for atom in model.atoms(Model.ATOMS):
            if (atom.name() == "pos" and len(atom.args()) == 4 and atom.args()[3] == self.horizon):
                self.last_positions.append(Fun("pos", atom.args()[:-1]))
horizon = 15
encodings = ["board.lp", "targets.lp", "ricochet.lp", "optimization.lp"]
positions = [Fun("pos", [Fun("red"),
                                       1, 1]), Fun("pos", [Fun("blue"),
                                                                              1. 16]).
            Fun("pos", [Fun("green"), 16, 1]), Fun("pos", [Fun("yellow"), 16, 16])]
sequence = [Fun("goal", [13]), Fun("goal", [4]), Fun("goal", [7])]
player = Player(horizon, positions, encodings)
for goal in sequence:
    print player.solve(goal)
```

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Storing stable model



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```

1 Storing stable model



ricochet.py

```
from gringo import Control, Model, Fun
class Plaver:
    def __init__(self, horizon, positions, files):
        self.last_positions = positions
        self.last_solution = None
        self.undo external = []
        self.horizon = horizon
        self.ctl = Control(['-c', 'horizon={0}'.format(self.horizon)])
        for x in files:
            self.ctl.load(x)
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    def solve(self, goal):
        for x in self.undo_external:
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        self.undo external = []
        for x in self.last_positions + [goal]:
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        self.last_solution = None
        self.ctl.solve(on model=self.on model)
        return self.last_solution
    def on model(self, model);
        self.last_solution = model.atoms()
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        for atom in model.atoms(Model.ATOMS):
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horizon = 15
encodings = ["board.lp", "targets.lp", "ricochet.lp", "optimization.lp"]
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sequence = [Fun("goal", [13]), Fun("goal", [4]), Fun("goal", [7])]
player = Player(horizon, positions, encodings)
for goal in sequence:
    print player.solve(goal)
```



\$ python ricochet.py

[move(red,0,1,1), move(yellow,-1,0,14), move(yellow,-1,0,12), move(yellow,-1,0,11), move(yellow,-1,0,9), move(red,1,0,7), move(red,1,0,2), move(yellow,-1,0,10), move(yellow,-1,0,13), move(yellow,-1,0,15), move(red,-1,0,4), move(yellow,0,-1,6), move(red,0,1,3), move(red,0,1,5), move(yellow,0,1,8)] [move(blue,0,1,15), move(blue,0,1,11), move(blue,0,1,8), move(blue,0,1,3), move(blue,0,1,13), move(blue,0,1,9), move(blue,-1,0,7), move(blue,0,1,10), move(blue,0,1,13), move(blue,-1,0,4), move(blue,0,-1,1), move(blue,0,-1,6), move(green,-1,0,5), move(blue,0,1,12), move(blue,0,1,14)] [move(green,1,0,15), move(green,1,0,8), move(green,1,0,5), move(green,1,0,4), move(green,1,0,3), move(green,1,0,10), move(green,1,0,11), move(green,1,0,12), move(green,1,0,6), move(green,1,0,14), move(green,0,1,1)]

\$./visualize.py

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🕼 gringo/clingo distribution ./examples/clingo/robots/

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\$ python ricochet.py [move(red,0,1,1), move(yellow,-1,0,14), move(yellow,-1,0,12), move(yellow,-1,0,11), move(yellow,-1,0,9), move(red,1,0,7), move(red,1,0,2), move(yellow,-1,0,10), move(yellow,-1,0,13), move(yellow,-1,0,15), move(red,-1,0,4), move(yellow,0,-1,6), move(red,0,1,3), move(red,0,1,5), move(yellow,0,1,8)] [move(blue,0,1,15), move(blue,0,1,11), move(blue,0,1,8), move(blue,0,1,3), move(blue,1,0,2), move(blue,0,1,9), move(blue,-1,0,7), move(blue,0,1,3), move(blue,0,1,13), move(blue,-1,0,4), move(blue,0,-1,1), move(blue,0,-1,6), move(green,-1,0,5), move(blue,0,1,12), move(blue,0,1,14)] [move(green,1,0,15), move(green,1,0,8), move(green,1,0,5), move(green,1,0,4), move(green,1,0,9), move(green,1,0,10), move(green,1,0,7), move(green,1,0,12), move(green,1,0,6), move(green,1,0,14), move(green,0,1,1)]

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Outline

1 Introduction

- 2 Foundations
- 3 Modeling
- 4 Modeling and Controlling
- 5 Case-study: Ricochet Robots
- 6 Case-sketch: Preferences and optimization
 - 7 Potassco
- 8 Summary



- The identification of preferred, or optimal, solutions is often indispensable in real-world applications
 In many cases, this also involves the combination of various
 - qualitative and quantitative preferences
- Only optimization statements representing objective functions using sum or count aggregates are established components of ASP systems
- Example #*minimize*{40 : *sauna*, 70 : *dive*}



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asprin is a framework for handling preferences among the stable models of logic programs

- general because it captures numerous existing approaches to preference from the literature
- flexible because it allows for an easy implementation of new or extended existing approaches
- asprin builds upon advanced control capacities for incremental and meta solving, allowing for

without any modifications to the

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Example

#preference(costs, less(weight)){40 : sauna, 70 : dive}
#preference(fun, superset){sauna, dive, hike, ~ bunji}
#preference(temps, aso){dive > sauna || hot, sauna > dive || ¬hot}
#preference(all, pareto){name(costs), name(fun), name(temps)}
#optimize(all)



asprin's library

Basic preference types

- subset and superset
- less(cardinality) and more(cardinality)
- less(weight) and more(weight)
- aso (Answer Set Optimization)
- poset (Qualitative Preferences)

Composite preference types

- neg
- and
- pareto
- lexico
- See Potassco Guide on how to define further types and http://potassco.sourceforge.net/labs.html#asprin



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Potassco, the Potsdam Answer Set Solving Collection, bundles tools for ASP developed at the University of Potsdam:

- Grounder gringo, lingo
- Solver clasp, claspfolio, claspar, aspeed
- Grounder+Solver Clingo, Clingcon, ROSoClingo
- Further Tools aspartame, aspcud, asprin, chasp, claspre, clavis, coala, fimo, insight, metasp, plasp, piclasp, etc

asparagus.cs.uni-potsdam.de



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- ASP offers an expanding functionality and ease of use
 - rapid application development tool
- ASP has a growing range of applications



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